

# Low Precision Inference and Training for Deep Neural Networks

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THE UNIVERSITY OF  
SYDNEY

**CruxML**  
REAL-TIME COMPUTING & MACHINE LEARNING



# Computer Engineering Laboratory

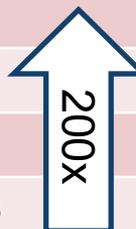
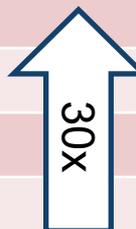
- › Focuses on how to use parallelism to solve demanding problems
  - Novel architectures, applications and design techniques using FPGAs
- › Research: reconfigurable computing, radio frequency machine learning



## Tradeoff between performance and precision

- › CPUs/GPUs designed to support datatypes of fixed wordlength
  - Double, float, long, short, char
- › FPGA and ASICs can provide custom datapaths of arbitrary wordlength

Precision	Peak TOPS	On-chip weights
1b	~66	~70 M
8b	~4	~10 M
16b	~1	~5 M
32b	~0.3	~2 M

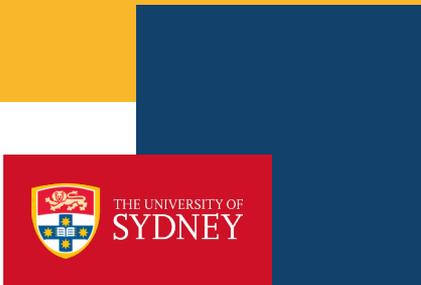



Slide: Xilinx

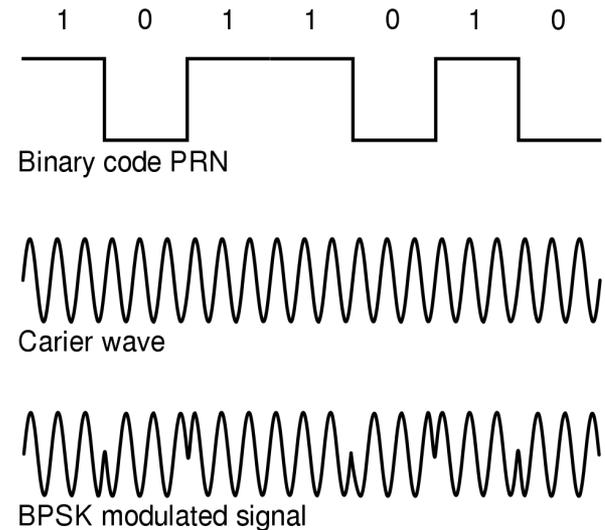
- › So how can we utilize low-precision for inference and training?

# Inference

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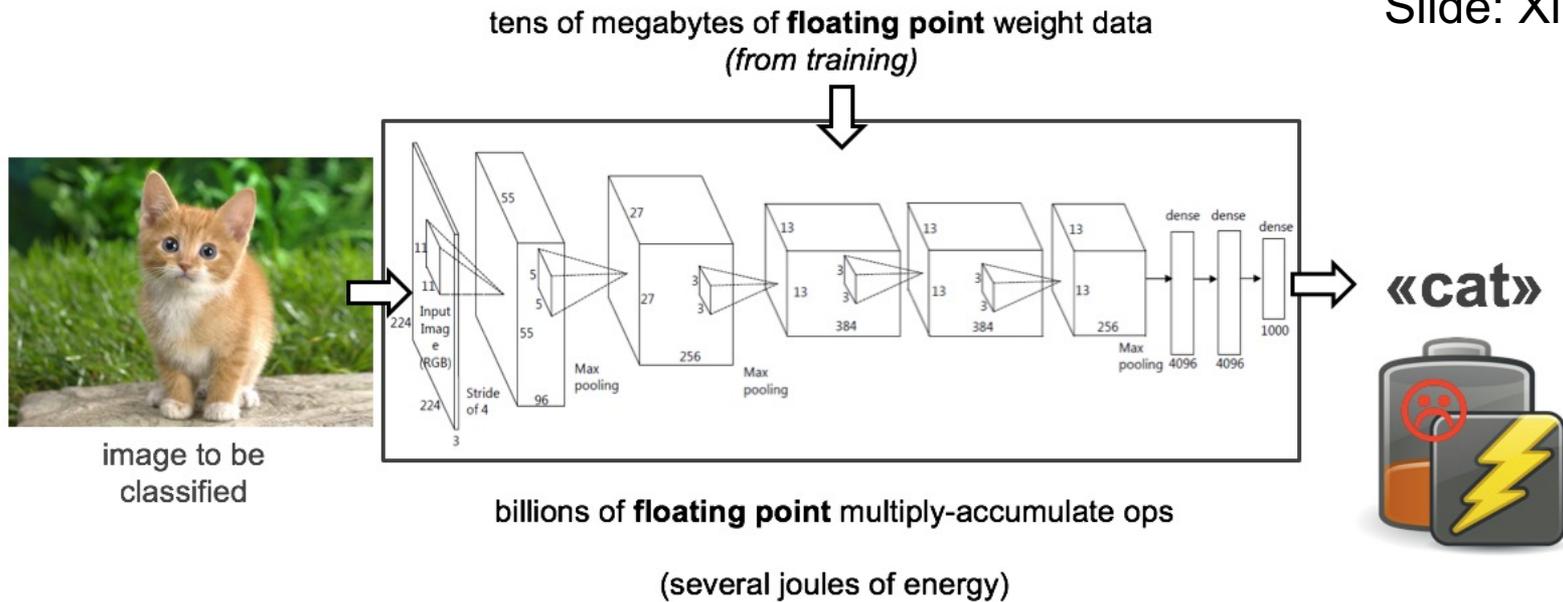


- › Understanding of radio signals in low SNR difficult problem
- › Radio data is high speed and low latency often required (ML will never be fast enough)
- › FPGAs offer possibility of integrating radio, signal processing and ML on the same chip
- › Study automatic modulation classification (AMC): detect modulation type from raw IQ samples
  - Other problems similar



# Background: Convolutional Neural Network

Slide: Xilinx

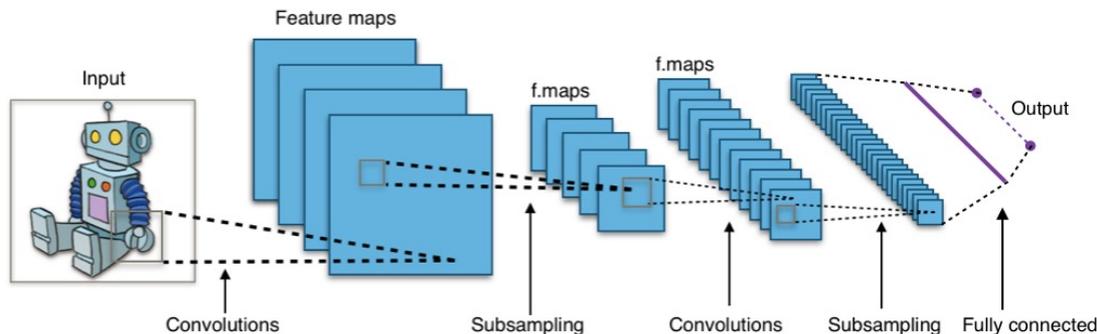


O'Shea et al, "Over-the-Air Deep Learning Based Radio Signal Classification"

- ResNet on the raw IQ data gives SOA results

FINN: A framework for fast, scalable binarized neural network inference,”  
FPGA’17

- › *Much* smaller datapaths
  - Multiply becomes XNOR, addition becomes popcount
  - No DSPs needed, everything in LUTs
- › *Much* smaller weights
  - Large networks can fit entirely into on-chip memory (OCM)



But accuracy not good! How can we improve accuracy and performance?

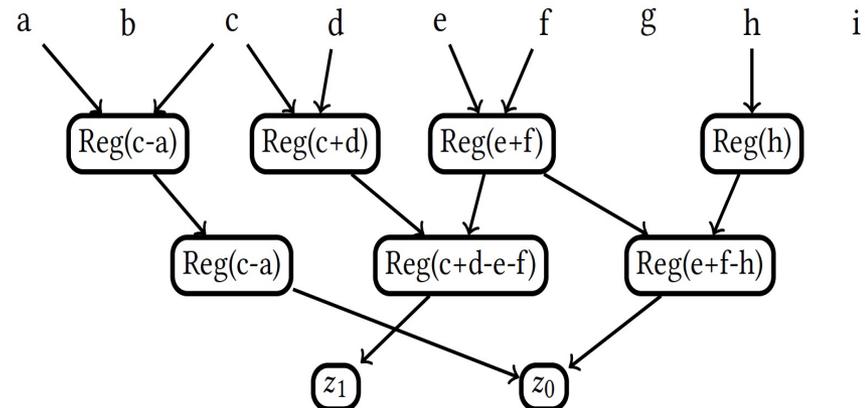
- › To achieve highest speed: parallel implementation (but FPGA resources insufficient for contemporary CNN model)
- › How can we push limits of performance on an FPGA?
- › Exploit unstructured sparsity and the following techniques:
  1. Massively parallel ternary NN implemented as pruned adder trees
  2. Common subexpression merging
  3. 16-bit bit serial arithmetic to minimize accuracy loss with low area
  4. Sparsity control (not discussed)

## > Weights are ternary

- Reduces convolution to constructing adder tree
- Subexpression merged to reduce implementation

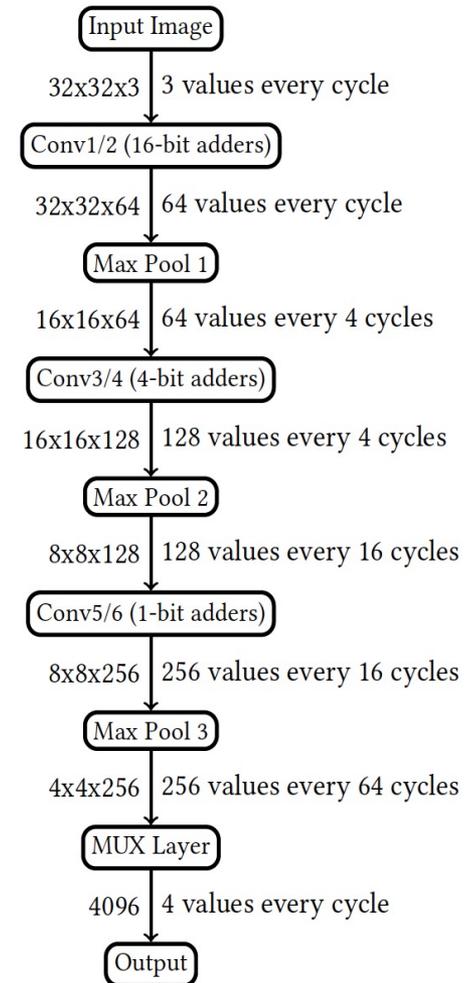
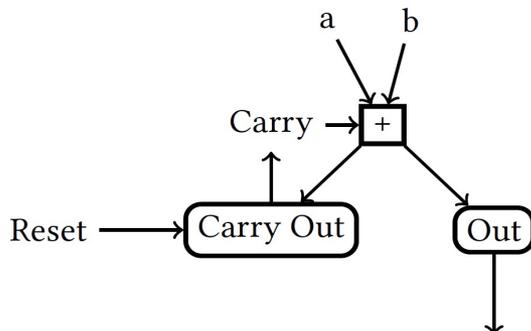
Computing  $z_0 = c + e + f - (a + h)$  and  $z_1 = c + d - e - f$

$$\begin{array}{lll}
 a \times (-1) & b \times 0 & c \times 1 \\
 d \times 0 & e \times 1 & f \times 1 \\
 g \times 0 & h \times (-1) & i \times 0
 \end{array}$$



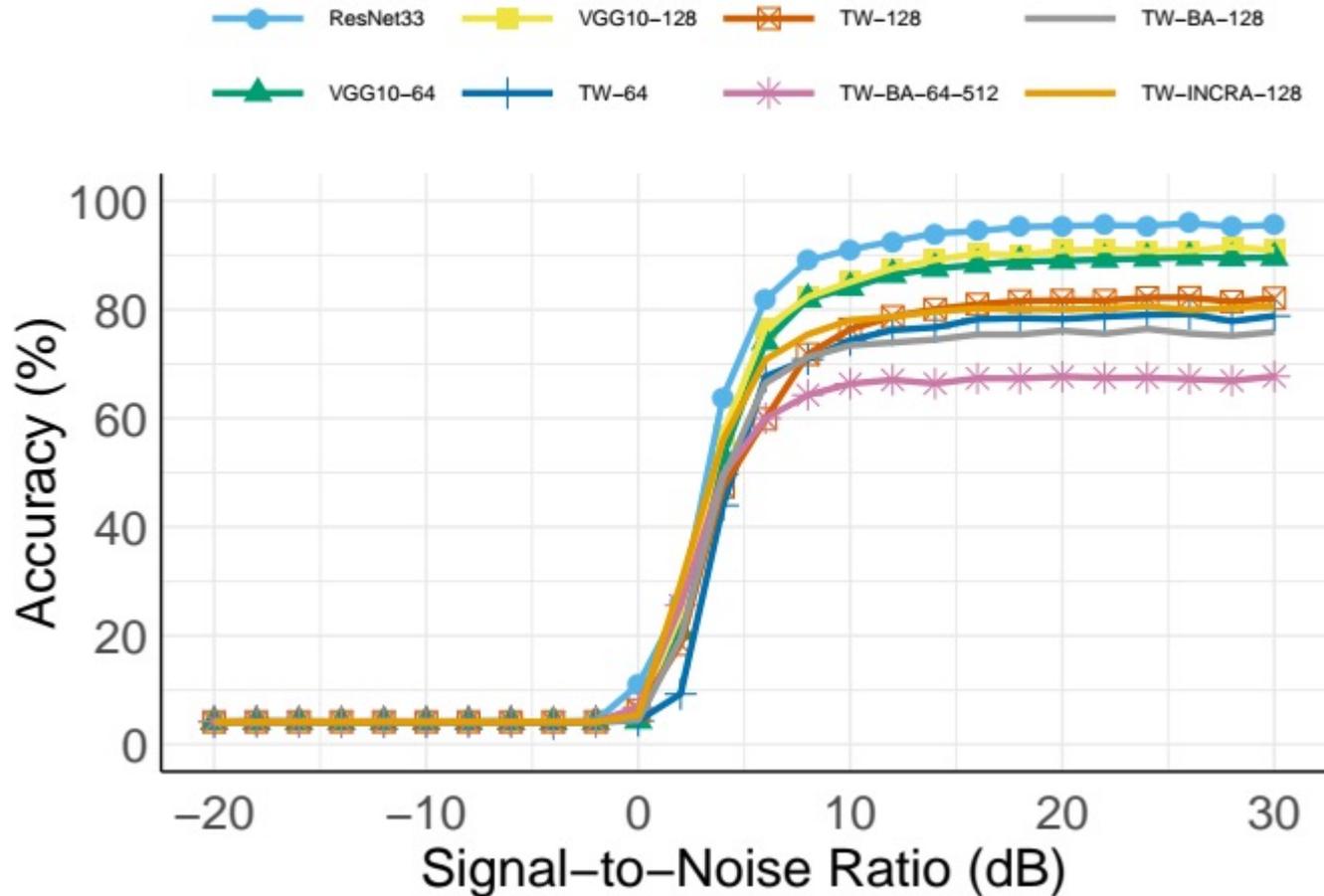
## > Activations are 16-bit

- Not all layers have same throughput
- Use digit serial to make more compact
- 4-bit digit serial has 1/4 area
- 1-bit bit serial has 1/16 area





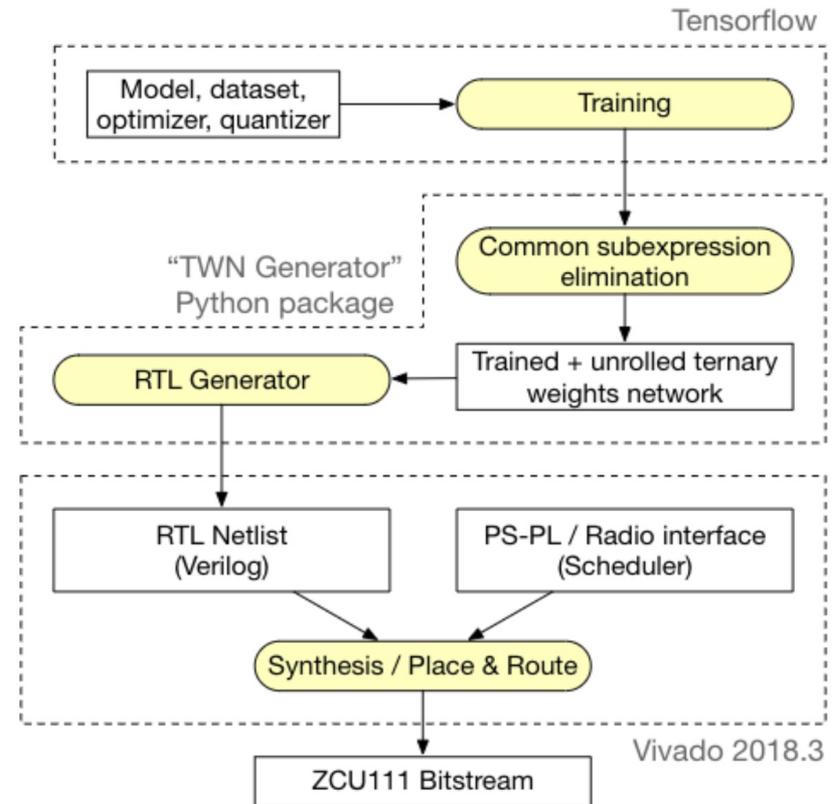
# Accuracy on RadioML 2018.01A dataset



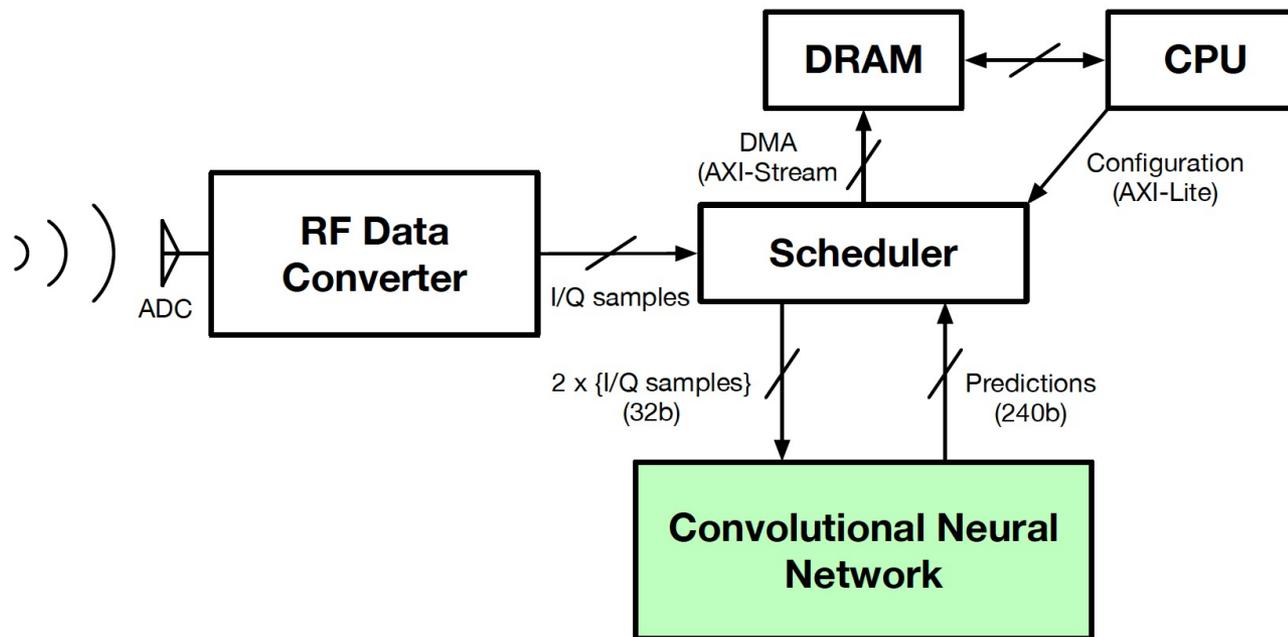
- > Use incremental precision activations instead of 16 bit everywhere (to improve accuracy)
  - Use bit serial adders everywhere
  - Adjust precision to match the throughput
  - Same area as binary activations
  - Almost 5% accuracy gain over binary activations

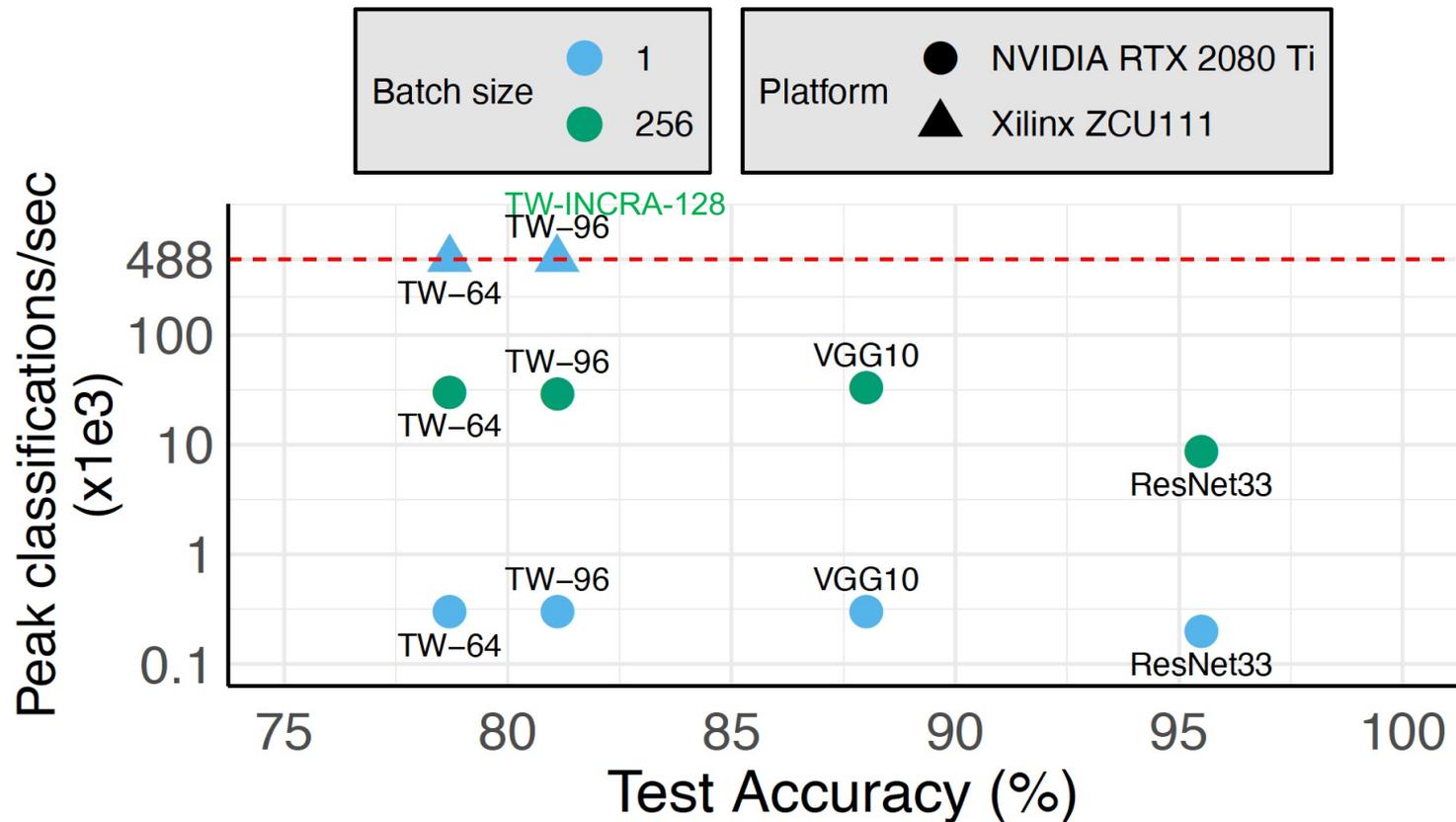
Model	TW-64	TW-96	TW-BA-128	TW-INCRA-128
CLBs	28k (53.5%)	47k (89.3%)	43k (80.7%)	42k (80.2%)
LUTs	124k (29.1%)	232k (54.7%)	234k (55.1%)	211k (49.6%)
FFs	217k (25.5%)	369k (43.4%)	333k (39.2%)	324k (38.1%)
BRAMs	524 (48.5%)	524 (48.5%)	523 (48.4%)	512.2 (48.3%)
DSPs	1496 (35%)	1207 (28.3%)	1408 (33.0%)	1407 (32.9%)
Accr	78.7	81.1	75.9	80.2

- › System implemented on ZCU111 RFSoc
- › [https://github.com/dastev101/radio\\_modulation](https://github.com/dastev101/radio_modulation)
- › Open Source Ternary Weight Network (TWN) Verilog generator
- › [https://github.com/dastev101/twn\\_generator](https://github.com/dastev101/twn_generator)

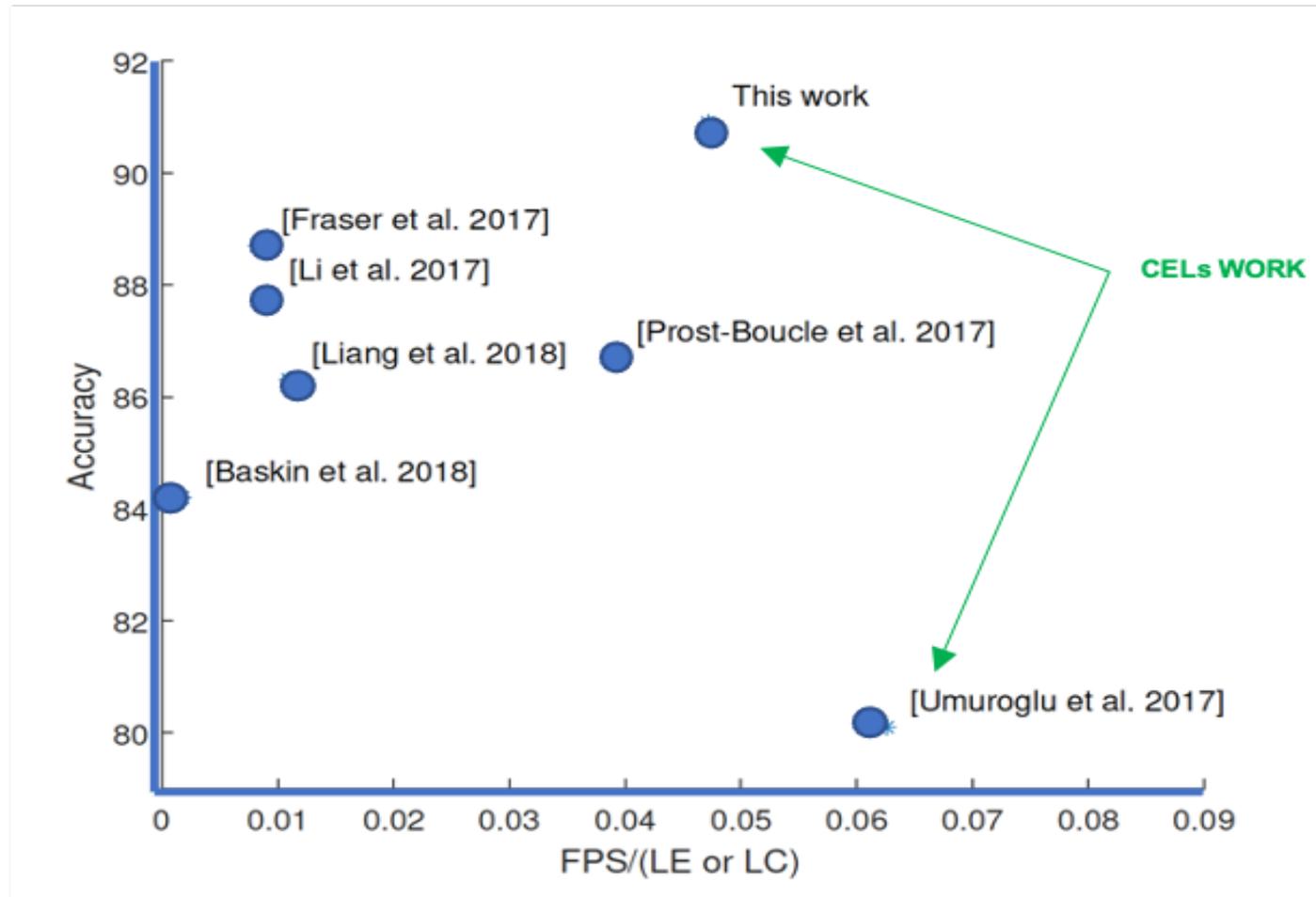


- › Automatic Modulation classifier: 488K class/s, 8us latency using TW-INCRE-128





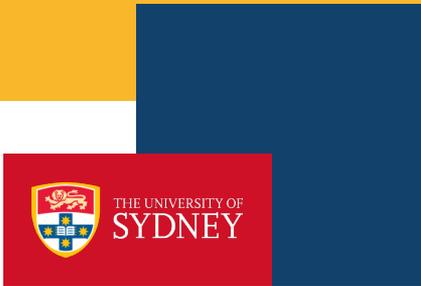
# Accuracy vs FPS/LE on CIFAR10 (not AMC)



- › Presented an optimized network for AMC which
  - Applies common subexpression elimination and digit serial arithmetic to a fully unrolled ternary network
  - Integrates the entire design on a single chip for a low-latency batch size 1 implementation
- › These serve to achieve a level of performance higher than previously reported
- › Further research needed to achieve state of the art accuracy with lower precision

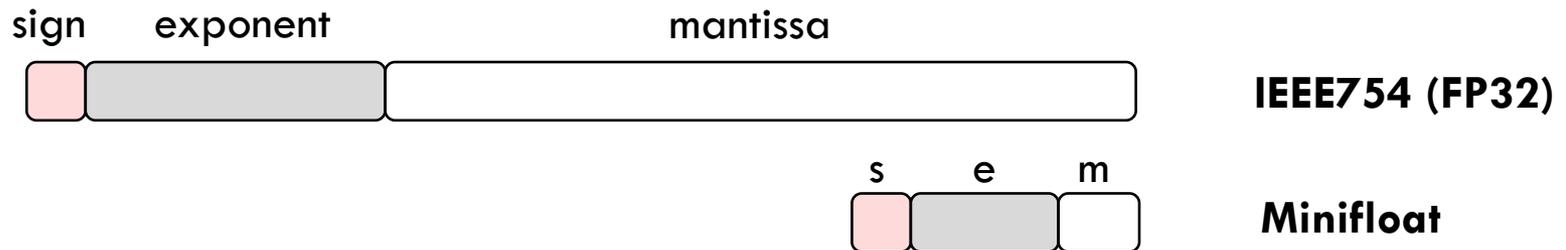
# Training

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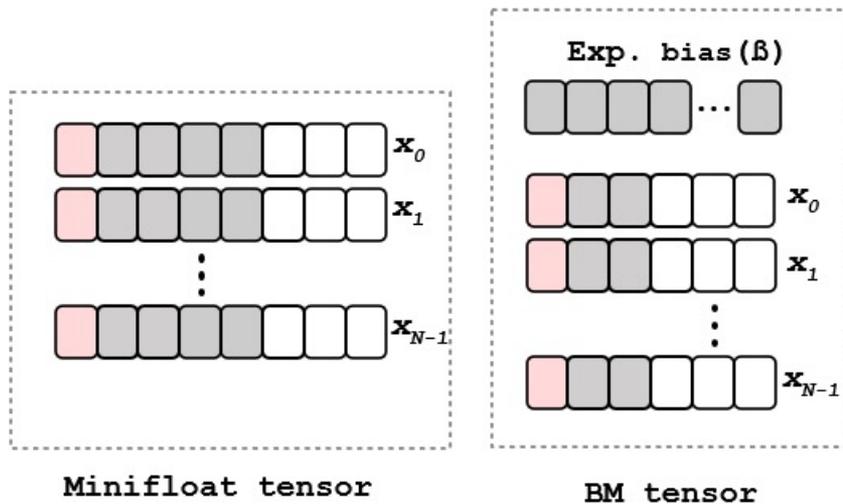
- Deep learning has even higher efficiency problem than inference!
    - E.g. Billions of parameters, 500+ GPUs
  - **Specialized number representations have been proposed**
    - Alternative to FP32/FP16
    - 4-8 bits for weights, activations and gradients
    - Cheaper and faster training systems
    - Datacenter to edge?
-

- Narrow floating-point representation
  - Ours range between 4-8 bits
  - NaN/Infinity NOT supported



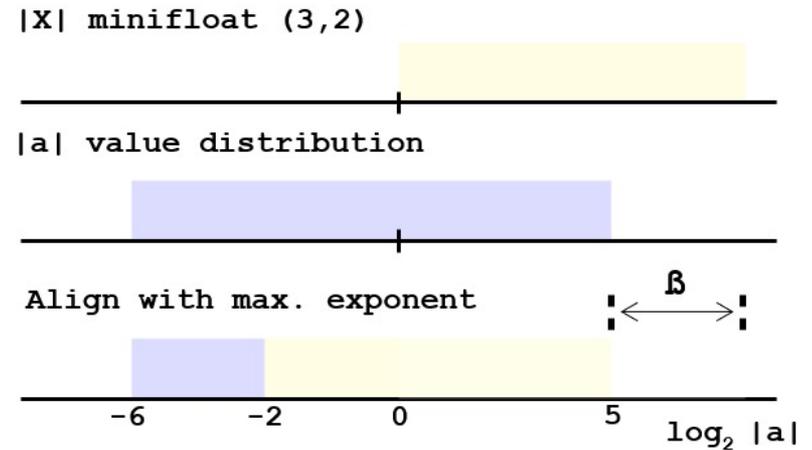
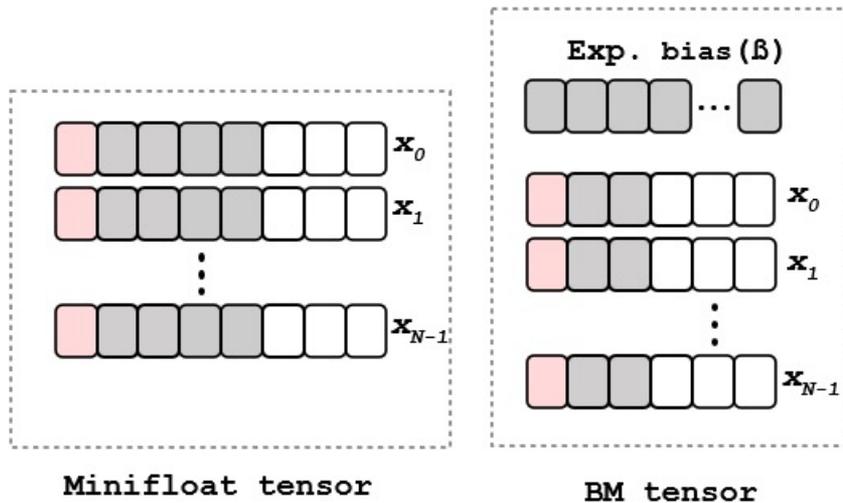
- Pros:
  - Memory (fewer bits)
  - Smaller hardware
- Cons:
  - Dynamic Range (exponent bits)  
**For training  $\geq 8$  bits**

- Share exponent bias across **blocks** of  $N$  minifloat numbers



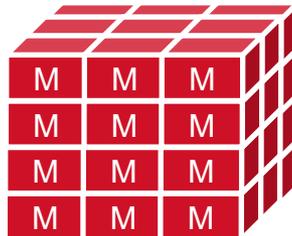
- Dynamic range (with fewer bits)
- Denser dot-products in hardware

- Share exponent bias across **blocks** of  $N$  minifloat numbers

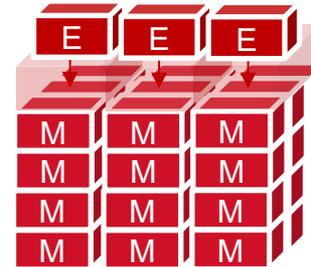


- Dynamic range (with fewer bits)
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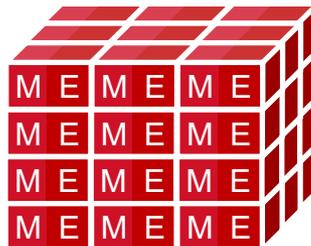
- Align with **max** exponent
- Underflow is tolerated



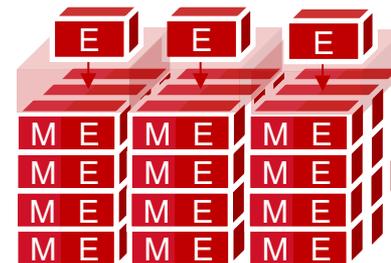
Fixed



BFP



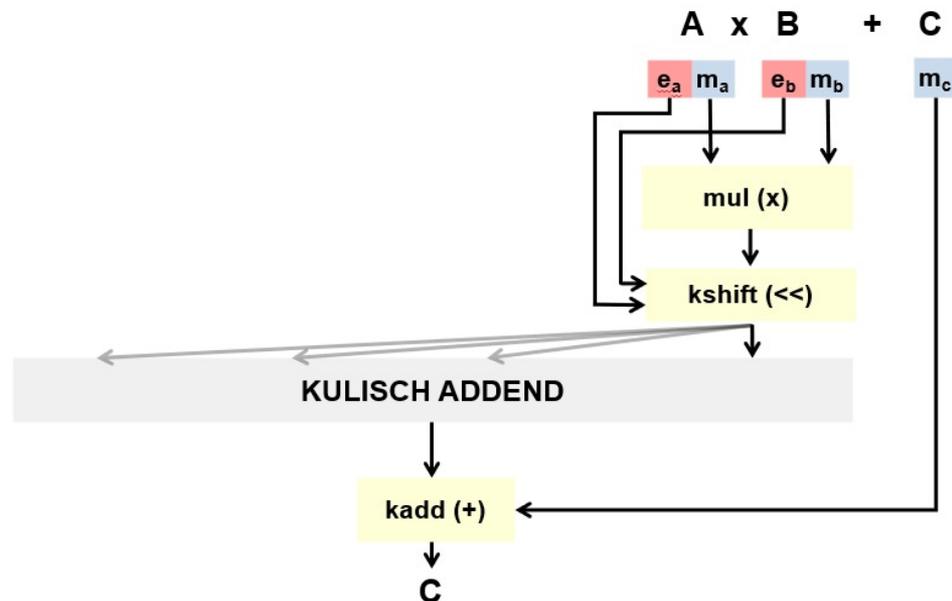
Minifloat



Block Minifloat

- Block Minifloats – share exponent bias across **blocks** of  $N$  minifloat numbers
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- **Kulisch Accumulator:** Fixed point accumulator wide enough to compute error-free sum of floating-point products
- Integer-like hardware complexity for **exponent  $\leq 4$  bits**

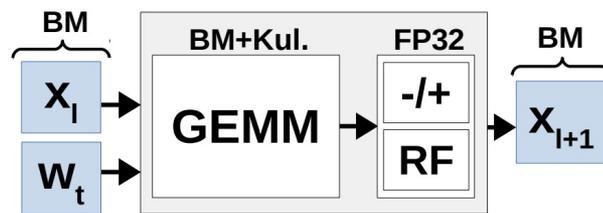


- Three techniques to reduce data loss:
  - Gradual underflow, Block Design, Hybrid Formats
- Simulate specialized BM hardware on GPU (with FP32)
  - Apply Block Minifloat to all weights, acts, grads
- Our Spectrum of Block Minifloats

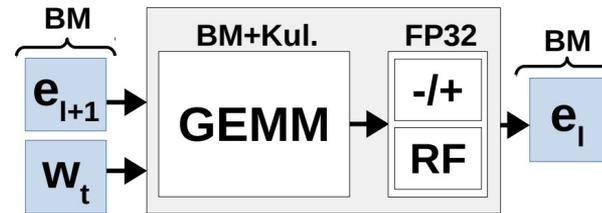
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BM8 (ours)	(2,5)/(4,3)
BM7 (ours)	(2,4)/(4,2)
BM6 (ours)	(2,3)/(3,2)
BM5 (ours)	(2,2)/(3,1)
BM5-log (ours)	(4,0)/(4,0)
BM4 (ours)	(2,1)/(3,0)
BM4-log (ours)	(3,0)/(3,0)

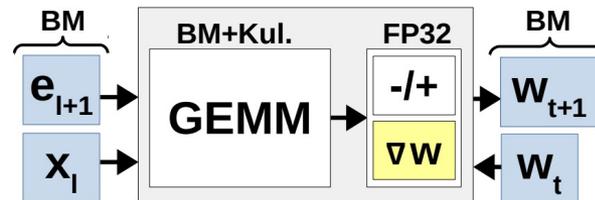
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(a) Fwd activation

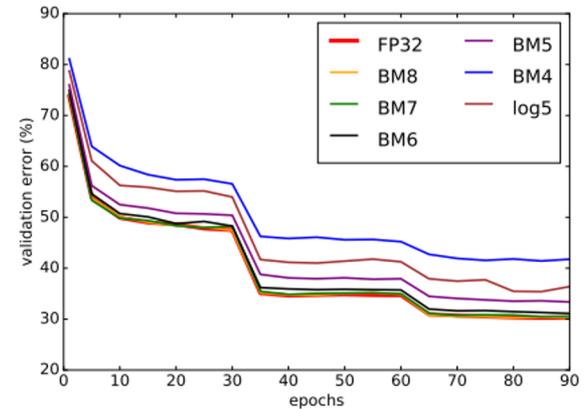


(b) Bwd activation grad.



(c) Bwd weight grad. and update

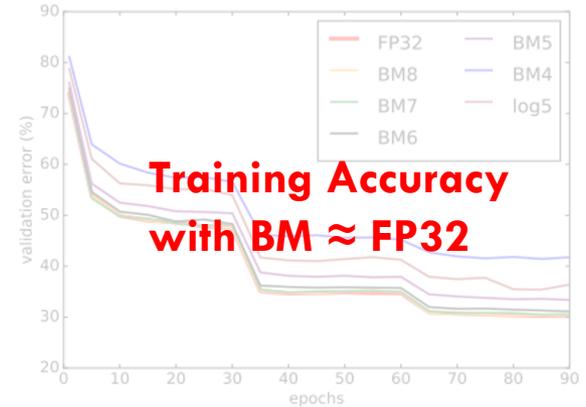
- **Training experiments:**
  - Datasets: (ImageNet, VOC, PTB, IWSLT)
  - Models: (ResNet, LSTM, TF base, SSD-Lite, EfficientNet)



- **RTL synthesis:**
  - Fused multiply-add (FMA)
  - 4x4 systolic matrix multipliers

Component	Area ( $\mu m^2$ )	Power ( $\mu W$ )
FP32	4782	10051
FP8 (w/ FP16 add)	829	1429
INT8 (w/ INT32 add)	417	1269
BM8	391	1141
BM6	<b>200</b>	<b>624</b>
INT8 (4x4 systolic)	7005	20253
FP8 (4x4 systolic)	18201	56202
BM8 (4x4 systolic)	<b>6976</b>	<b>18765</b>

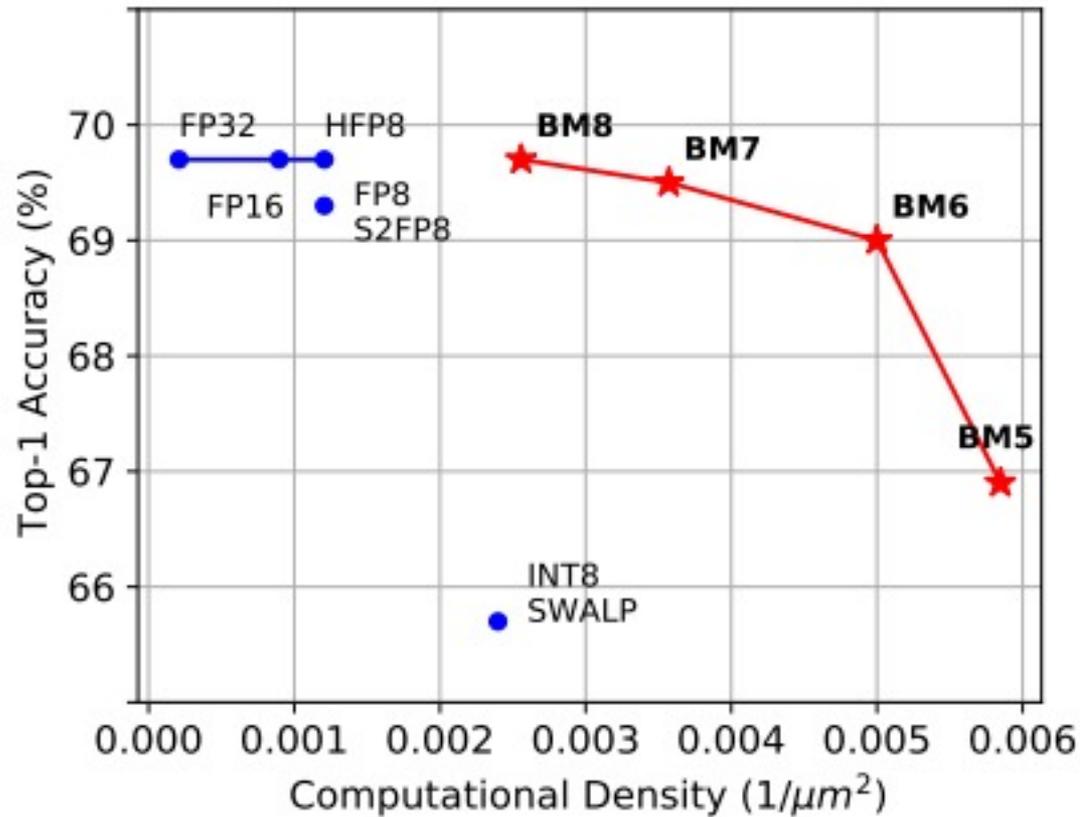
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**BM units are: Smaller, Consume less Power, Similar in area and power to FP8 with FP32 acc**



**Model: ResNet-18**  
**Dataset: ImageNet**

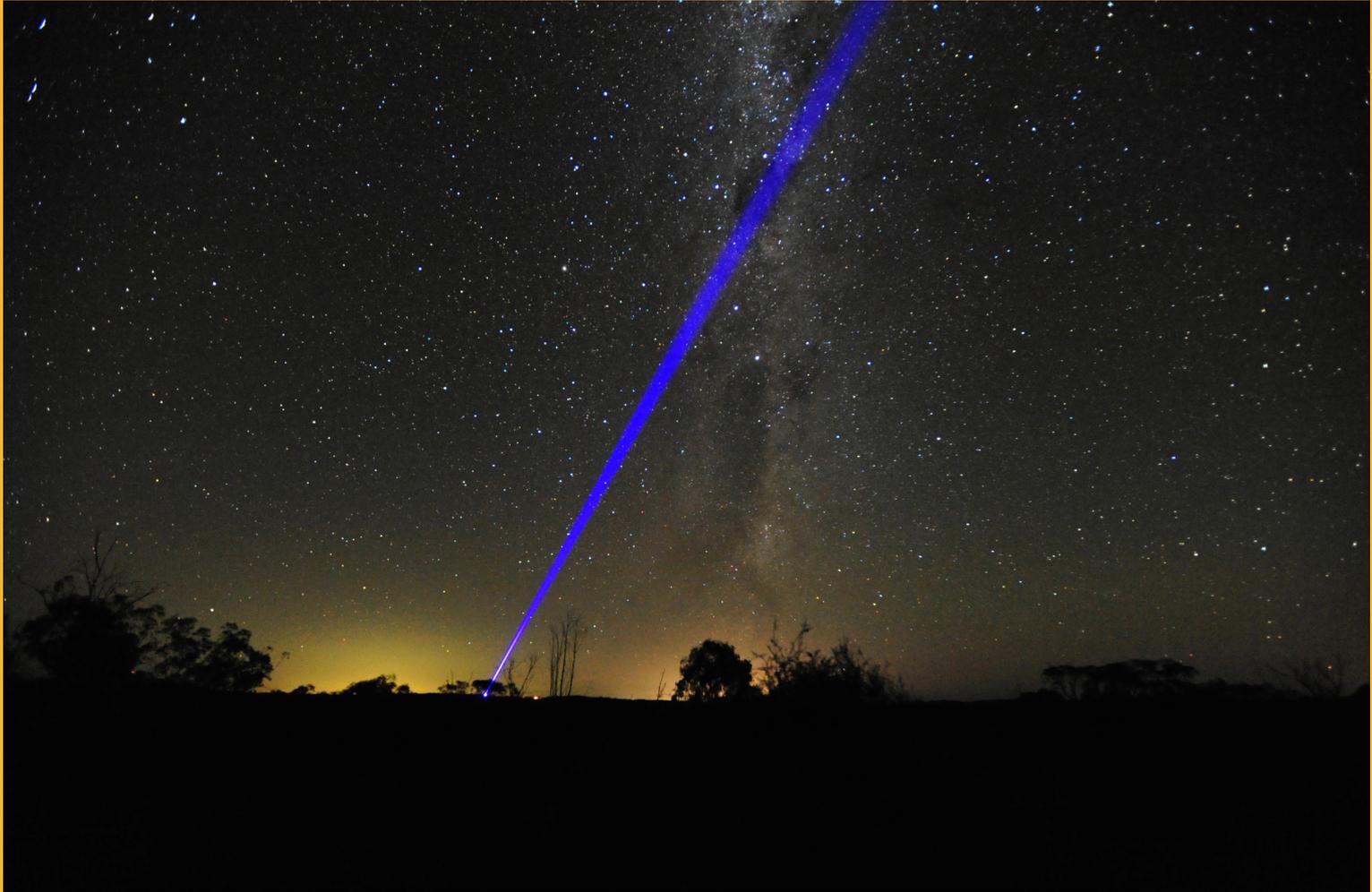
- Block Minifloat sustains high training accuracy with lower precision than previous techniques
  - Faster Training is possible:
    - Fewer bits – increases performance in memory-bound
    - Narrow exponents – yield denser arithmetic units in compute-bound
  - This work may be particularly advantageous in moving training into Edge devices
  - [github.com/sfox14/block\\_minifloat](https://github.com/sfox14/block_minifloat)
-

- › It is well known that DNN hardware performance can be significantly improved through precision optimisations
- › We have demonstrated feasibility of
  - Fully parallel, ternary single chip DNN implementations using adder trees, throughput matching and incremental activations
  - Training of wide variety of DNNs with single 8-bit precision format
- › More research needed to make this technology useful for mainstream applications

[1] Stephen Tridgell, David Boland, Philip HW Leong, Ryan Kastner, Alireza Khodamoradi, and Siddhartha. Real-time automatic modulation classification using RFSoc. In *2020 IEEE International Parallel and Distributed Processing Symposium Workshops, IPDPSW 2020, New Orleans, LA, USA, May 18-22, 2020*, 82–89. IEEE, 2020.

URL: [amc\\_raw20.pdf](#), [doi:10.1109 / IPDPSW50202.2020.00021](#).

[2] Sean Fox, Seyedramin Rasoulinezhad, Julian Faraone, and David Boland Philip H.W. Leong. A block minifloat representation for training deep neural networks. In *Proc. of The International Conference on Learning Representations (ICLR)*. 2021. URL: [bm\\_iclr21.pdf](#).



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