

Reconfigurable Computing

Parallelism

Indeed. RISC architecture is gonna change everything
- Angelina Jolie as Kate in Hackers

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- › Parallelism is the key to achieving high performance
- › We will cover two key techniques
 - Spatial parallelism (in 1 slide)
 - Pipelining
- › Case study
 - RISC processor

Parallelism



INPUT:
dirty laundry



OUTPUT:
6 more weeks



Device: Washer

Function: Fill, Agitate, Spin

$$\text{Washer}_{PD} = 30 \text{ mins} \\ = T_W$$



Device: Dryer

Function: Heat, Spin

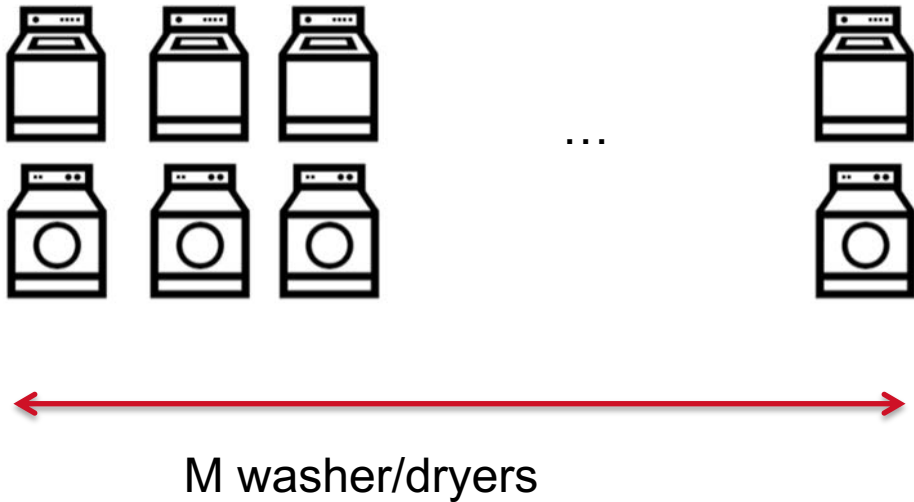
$$\text{Dryer}_{PD} = 60 \text{ mins} \\ = T_D$$

› Suppose we have N loads to process

› $\text{Time} = N(T_W + T_D)$

Figure by MIT OpenCourseware.

Spatially Parallel Laundry



- › If we had M washer dryers (and no other overheads)
- › $\text{Time} = (N/M)(\text{Washer} + \text{Dryer})$
- › But cost of equipment is also M times higher
- › (no dependencies i.e. all the loads can be operated in parallel)

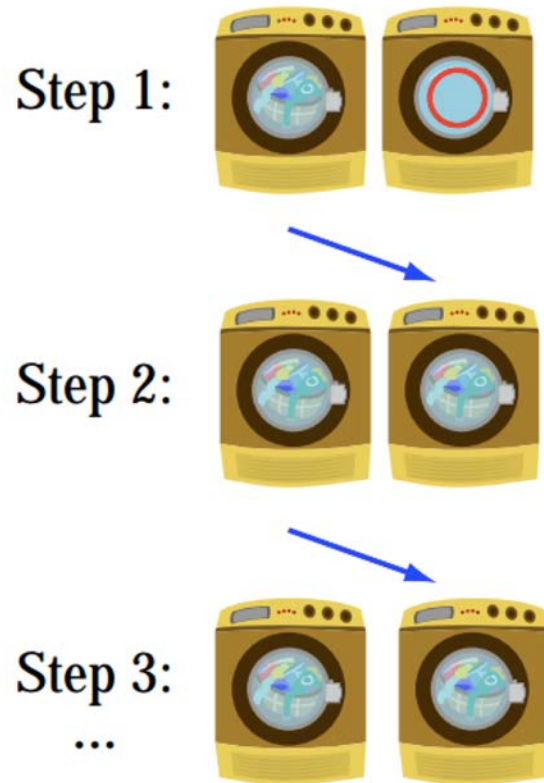


Figure by MIT OpenCourseware.

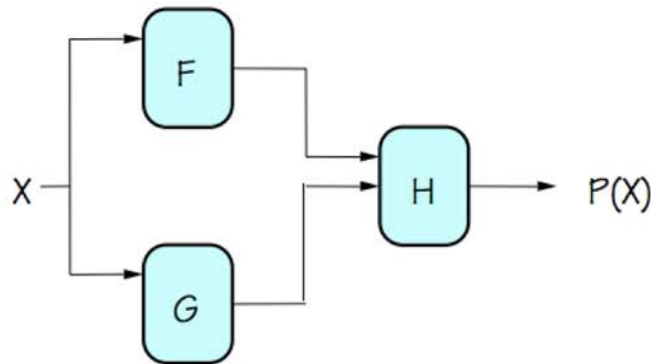
- › We can dry the first batch while we wash the second
- › Latency (time from when we supply the input to when the output is available)? $T_W + T_D$ (no change over seq)
- › Throughput (the rate at which inputs or outputs are processed)? $\max(T_W, T_D)$!
- › Time $\approx N \max(T_W, T_D)$
- › In general case for P stage pipeline to perform a task that takes time T
- › Speedup = $NT / ((P+N-1)T/P)$

$$= NP / (P+N-1)$$
- › As N becomes big, Speedup $\approx P$ (assuming that the cycle time is reduced from T to T/P)

Pipelining



Pipelining of Combinational Logic

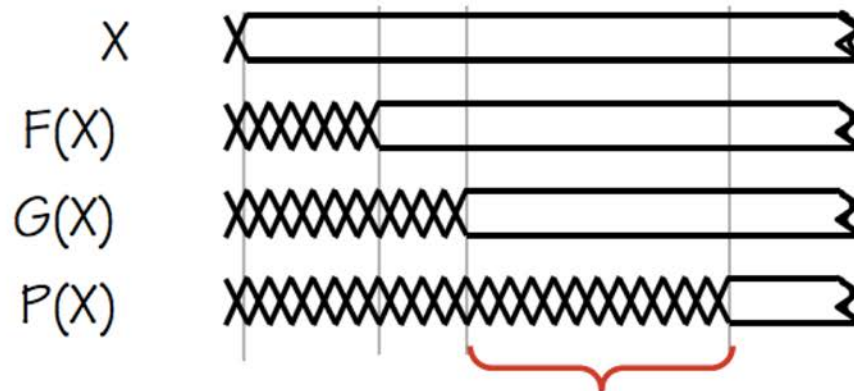


For combinational logic:

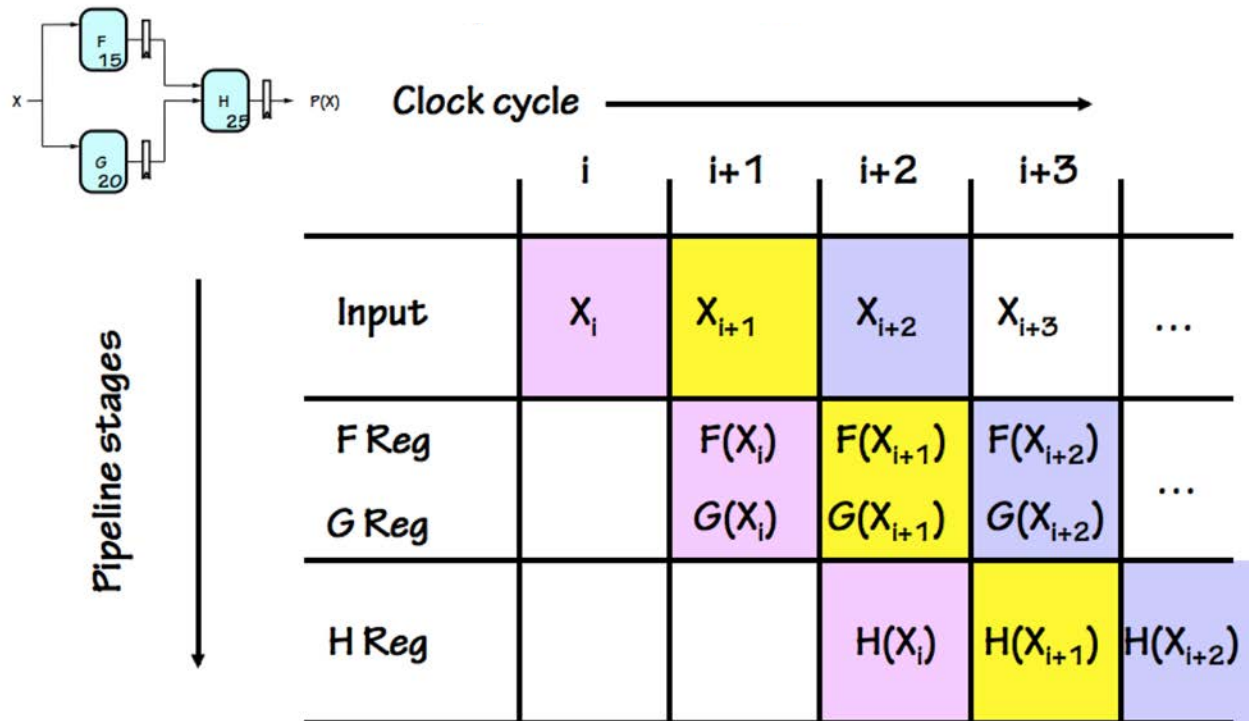
$$\text{latency} = t_{PD}$$

$$\text{throughput} = 1/t_{PD}$$

We can't get the answer faster, but
are we making effective use of our
hardware at all times?

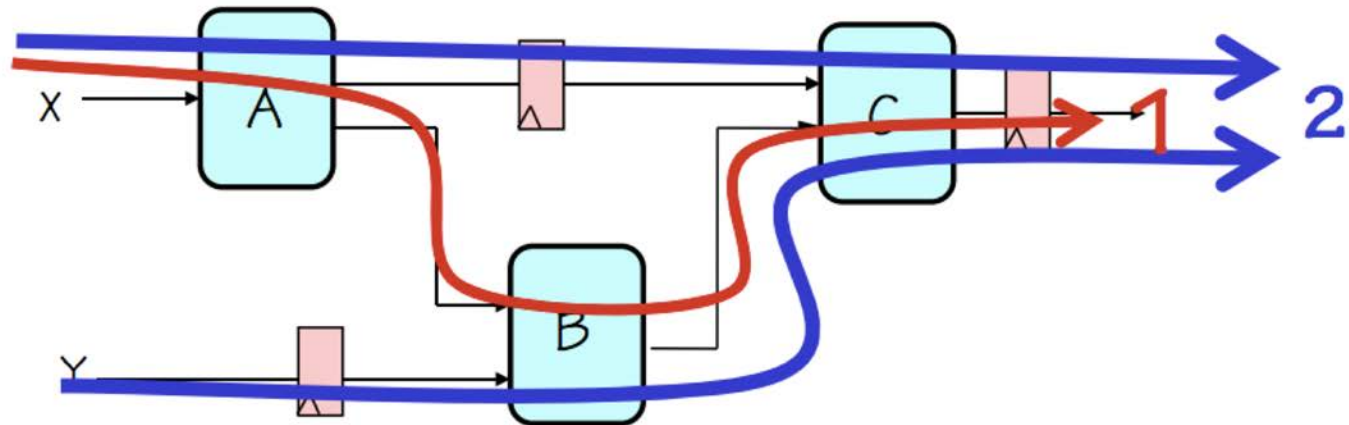


**F & G are "idle", just holding their outputs
stable while H performs its computation**



The results associated with a particular set of input data moves *diagonally* through the diagram, progressing through one pipeline stage each clock cycle.

Consider a BAD job of pipelining:

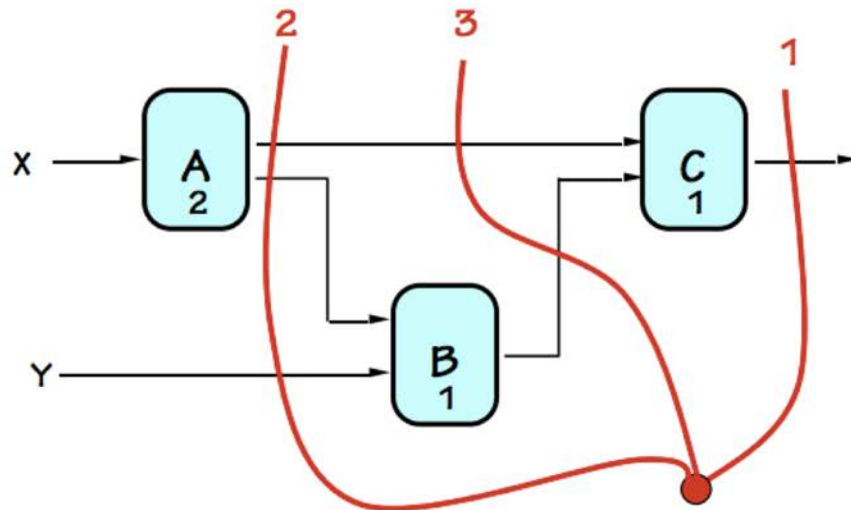


For what value of K is the following circuit a K-Pipeline? ANS: none

Problem:

Successive inputs get mixed: e.g., $B(A(X_{i+1}), Y_i)$. This happened because some paths from inputs to outputs have 2 registers, and some have only 1!

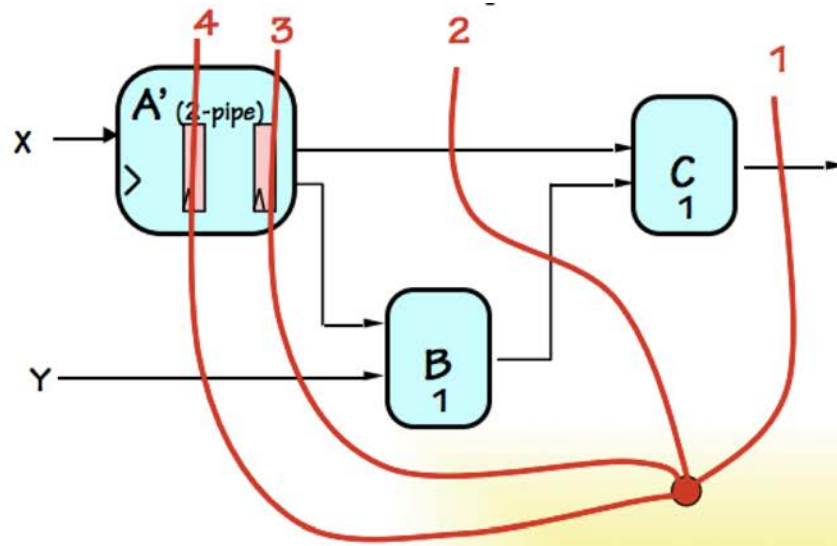
This CAN'T HAPPEN on a well-formed K pipeline!



OBSERVATIONS:

- 1-pipeline improves neither L or T.
- T improved by breaking long combinational paths, allowing faster clock.
- Too many stages cost L, don't improve T.
- Back-to-back registers are often required to keep pipeline well-formed.

	LATENCY	THROUGHPUT
0-pipe:	4	1/4
1-pipe:	4	1/4
2-pipe:	4	1/2
3-pipe:	6	1/2



4-stage pipeline, thruput=1

but... but...
How can I pipeline
a clothes dryer???

Pipelined systems can be hierarchical:

- Replacing a slow combinational component with a k-pipe version may increase clock frequency
- Must account for new pipeline stages in our plan

Recall our earlier example...

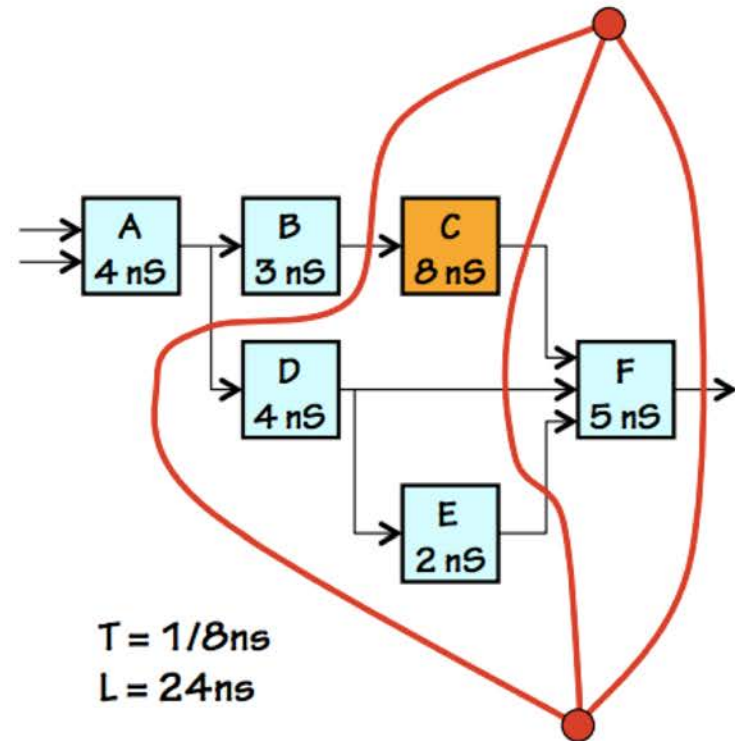
- *C* – the slowest component – limits clock period to 8 ns.
- HENCE throughput limited to $1/8\text{ns}$.

We could improve throughput by

- Finding a pipelined version of *C*;

OR...

- *interleaving* multiple copies of *C*!

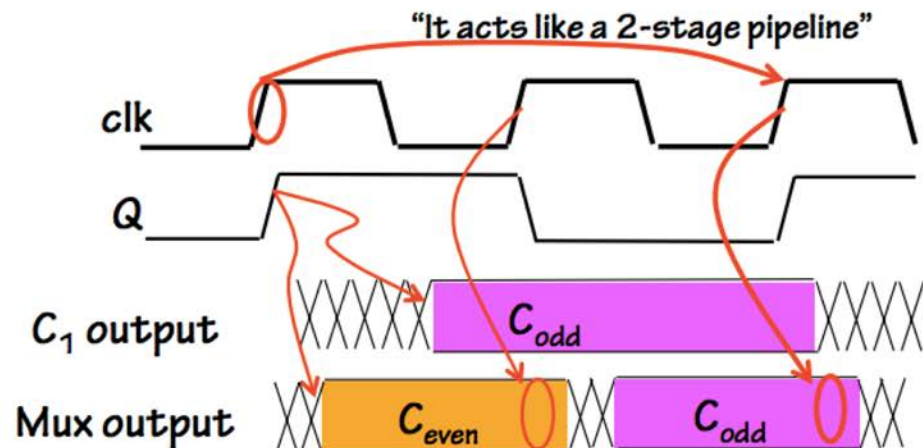
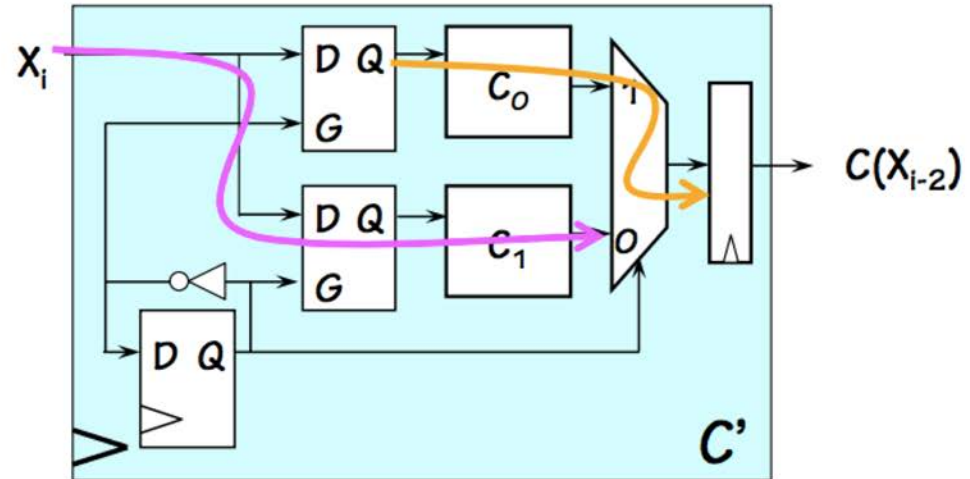


Circuit Interleaving (Pipelining + Spatial Parallelism)

We can simulate a pipelined version of a slow component by replicating the critical element and alternate inputs between the various copies.

When Q is 1 the lower path is combinational (the latch is open), yet the output of the upper path will be enabled onto the input of the output register ready for the NEXT clock edge.

Meanwhile, the other latch maintains the input from the last clock.

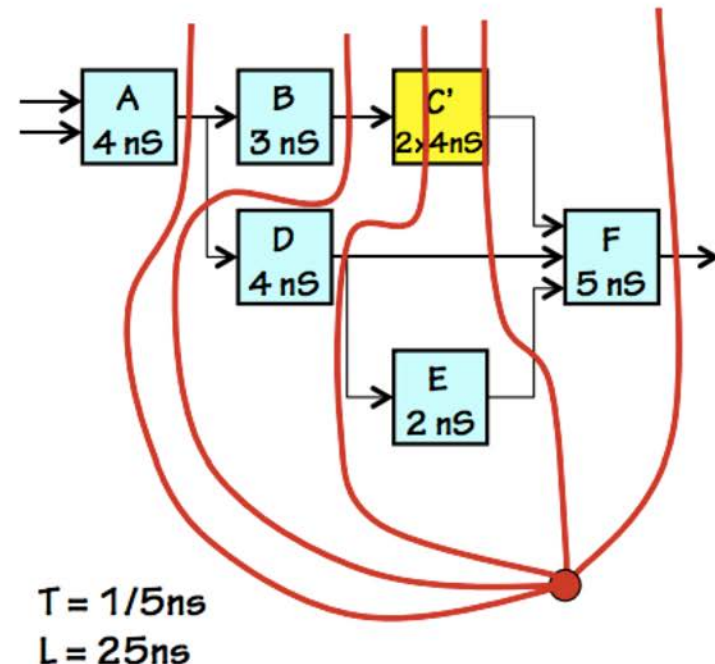


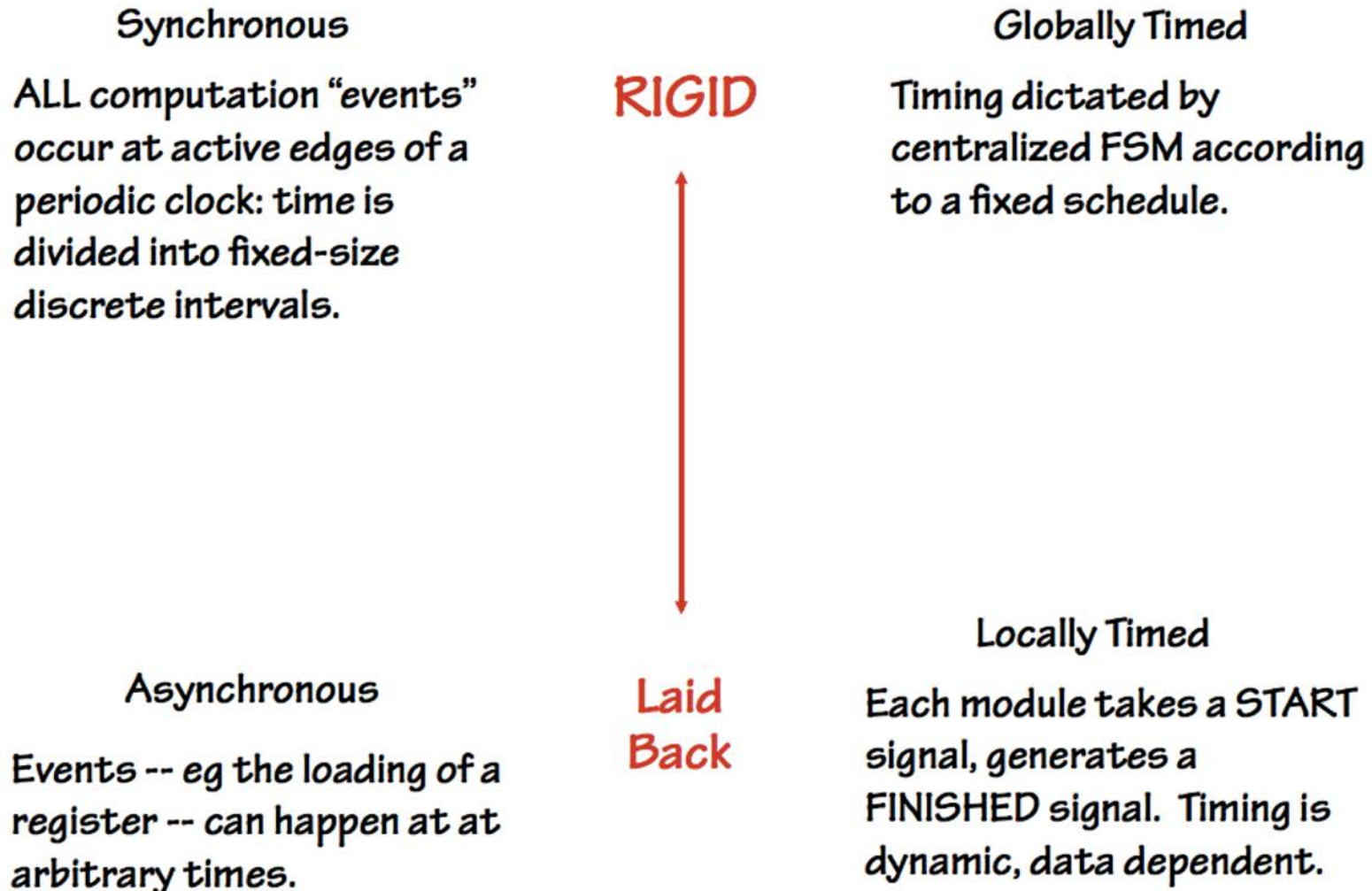
Combining Interleaving and Pipelining

We can combine interleaving and pipelining. Here, C' interleaves two C elements with a propagation delay of 8 nS .

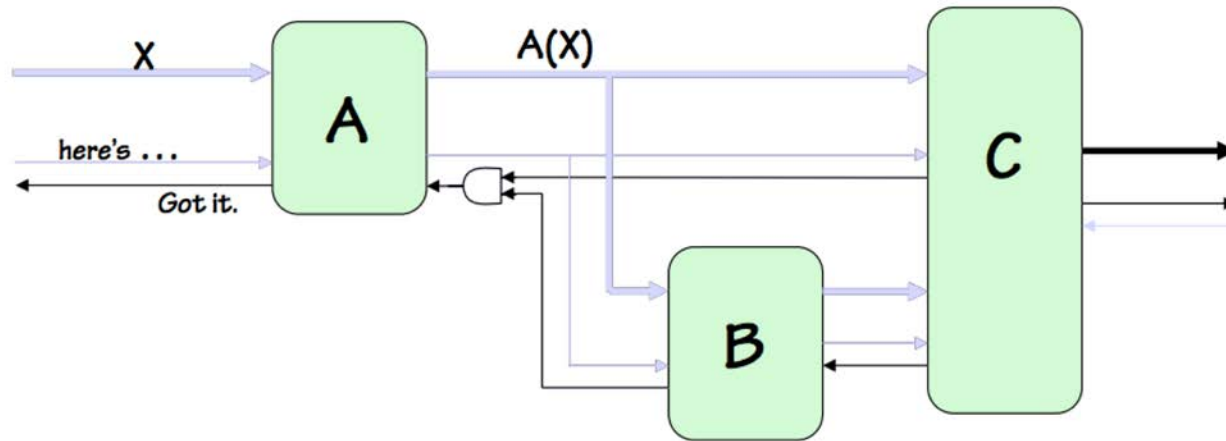
The resulting C' circuit has a throughput of $1/4\text{ nS}$, and latency of 8 nS . This can be considered as an extra pipelining stage that passes through the middle of the C' module. One of our separation lines must pass through this pipeline stage.

By combining interleaving with pipelining we move the bottleneck from the C element to the F element.





a glimpse of an asynchronous, locally-time discipline



Elegant, timing-independent design:

- **Each component specifies its own time constraints**
- **Local adaptation to special cases (eg, multiplication by 0)**
- **Module performance improvements automatically exploited**
- **Can be made asynchronous (no clock at all!) or synchronous**

- Latency (L) = time it takes for given input to arrive at output
- Throughput (T) = rate at each new outputs appear
- For combinational circuits: $L = t_{PD}$ of circuit, $T = 1/L$
- For K -pipelines ($K > 0$):
 - always have register on output(s)
 - K registers on every path from input to output
 - Inputs available shortly after clock i , outputs available shortly after clock $(i+K)$
 - $T = 1/(t_{PD,REG} + t_{PD}$ of slowest pipeline stage $+ t_{SETUP})$
 - more throughput \rightarrow split slowest pipeline stage(s)
 - use replication/interleaving if no further splits possible
 - $L = K / T$
 - pipelined latency \geq combinational latency

- › Techniques not discussed in this lecture but often used in reconfigurable computing
 - Vectorization
 - Systolic arrays
 - Task-level parallelism (particularly MPI)

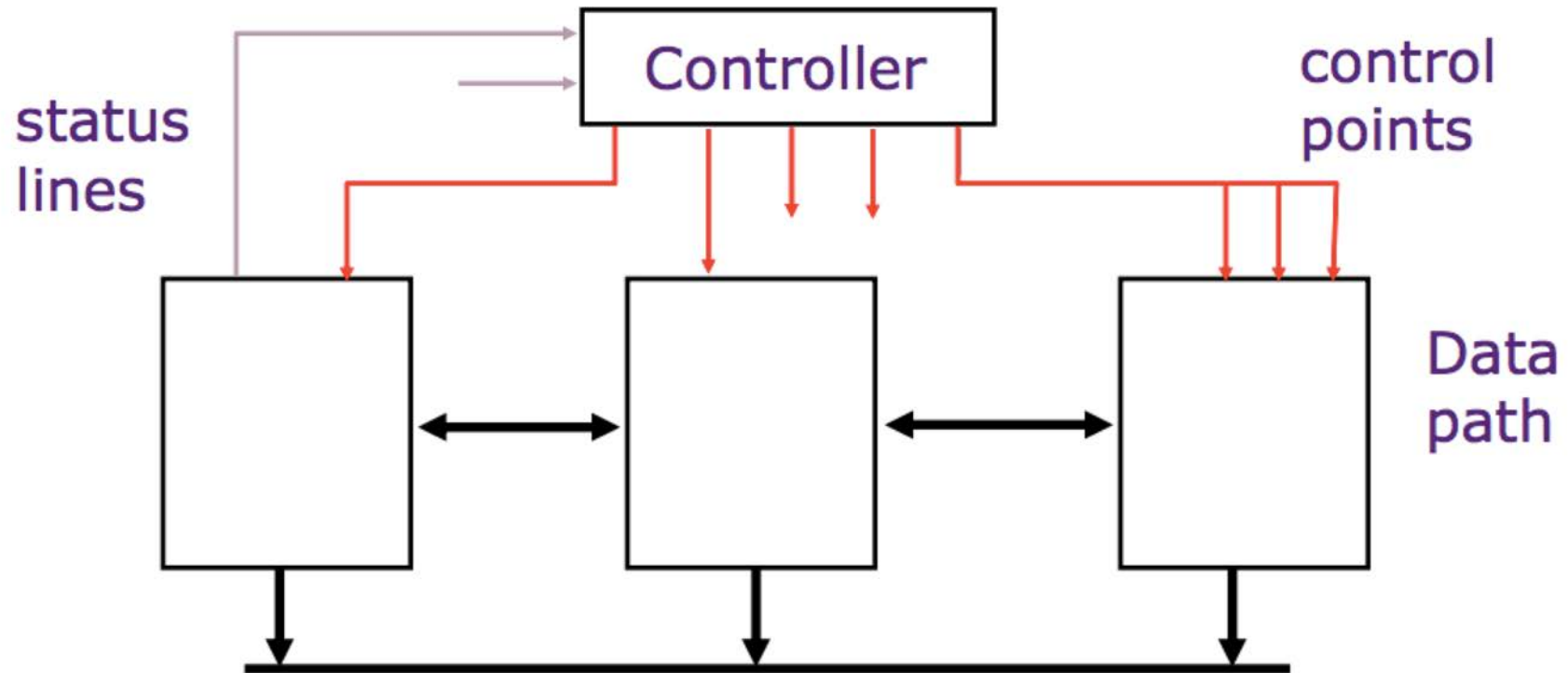
Single Cycle Processor - Datapath



- › Example of a design based on datapath+control with synchronous control
 - › Discuss the design of a reduced instruction set (RISC) processor for the MIPS instruction set
 - › The design methodology for any field-programmable custom computing machine (FCCM) is similar
 - Those without programmability are a special case of processors
 - › There are several different design methodologies, we cover single cycle first and then pipelined
-

$$\frac{\text{Time}}{\text{Program}} = \frac{\text{Instructions}}{\text{Program}} * \frac{\text{Cycles}}{\text{Instruction}} * \frac{\text{Time}}{\text{Cycle}}$$

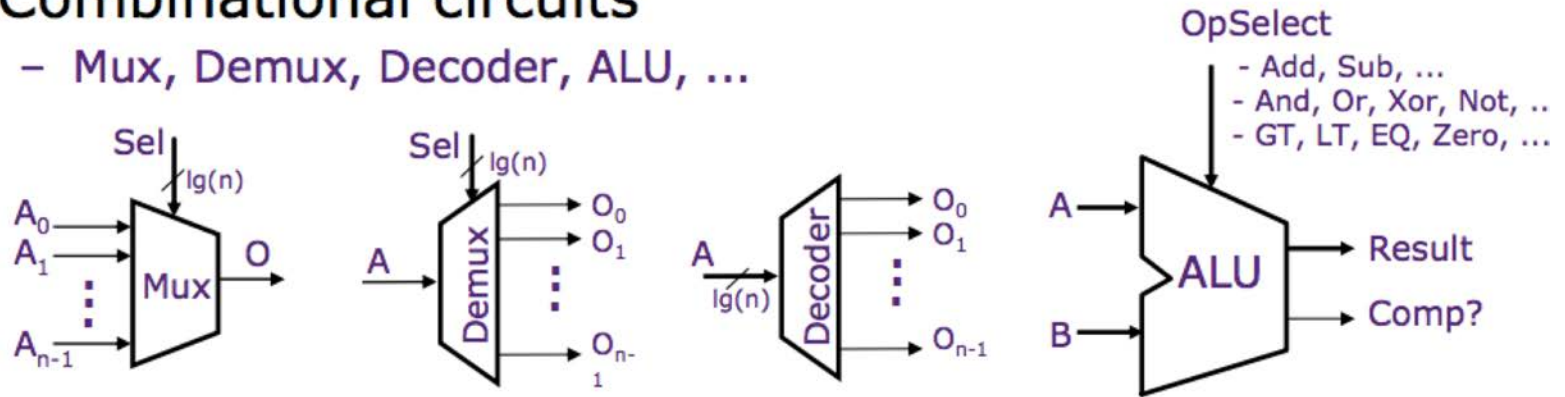
- › Instructions/Program function of source code, compiler and instruction set architecture (ISA)
- › Cycles/Instruction (CPI) function of ISA and microarchitecture
- › Time/Cycle depends on microarchitecture and the VLSI technology used



- › Structure: How components are connected (static)
- › Behaviour: How data moves between components (dynamic)

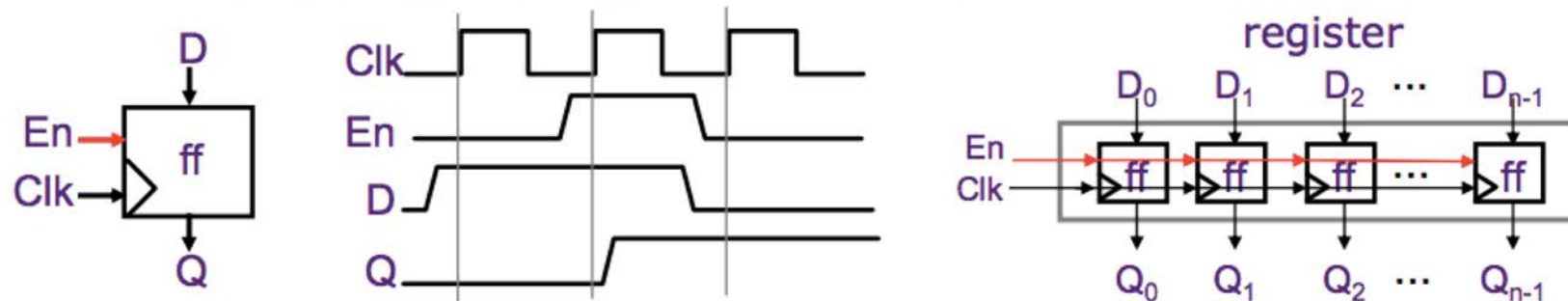
- **Combinational circuits**

- Mux, Demux, Decoder, ALU, ...

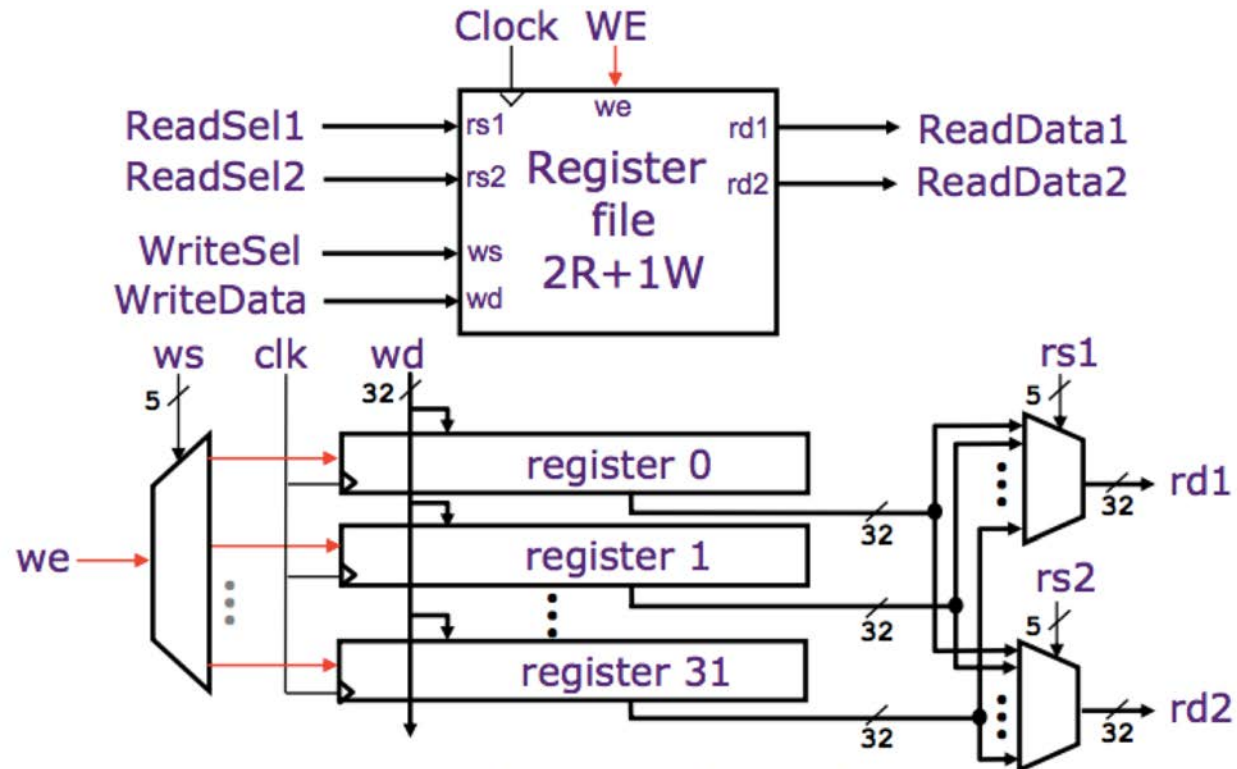


- **Synchronous state elements**

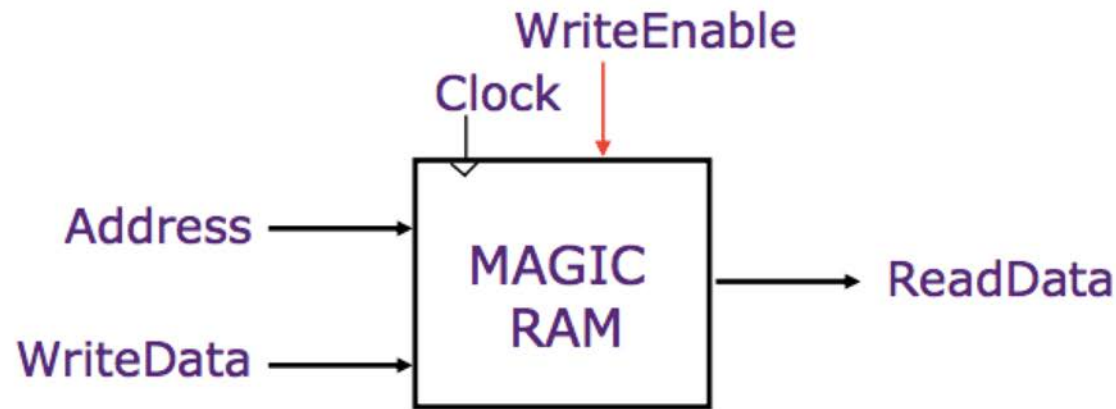
- Flipflop, Register, Register file, SRAM, DRAM



Edge-triggered: Data is sampled at the rising edge



- No timing issues in reading a selected register
- Register files with a large number of ports are difficult to design
 - Intel's Itanium, GPR File has 128 registers with 8 read ports and 4 write ports!!!



- Reads and writes are always completed in one cycle
- a Read can be done any time (i.e. combinational)
 - a Write is performed at the rising clock edge if it is enabled
- ⇒ the write address and data must be stable at the clock edge

Single Cycle RISC Processor



› Processor State

- 32 32-bit GPRs, R0 always contains a 0
- 32 single precision FPRs, may also be viewed as 16 double precision FPRs, FP status register, used for FP compares & exceptions
- PC, the program counter
- some other special registers

› Data types

- 8-bit byte, 16-bit half word
- 32-bit word for integers
- 32-bit word for single precision floating point, 64-bit word for double precision floating point

› Load/Store style instruction set

- data addressing modes- immediate & indexed
- branch addressing modes- PC relative & register indirect
- Byte addressable memory- big endian mode

› All instructions are 32 bits

R-type:

op	rs	rt	rd		func
----	----	----	----	--	------

I-type:

op	rs	rt	immediate16
----	----	----	-------------

J-type:

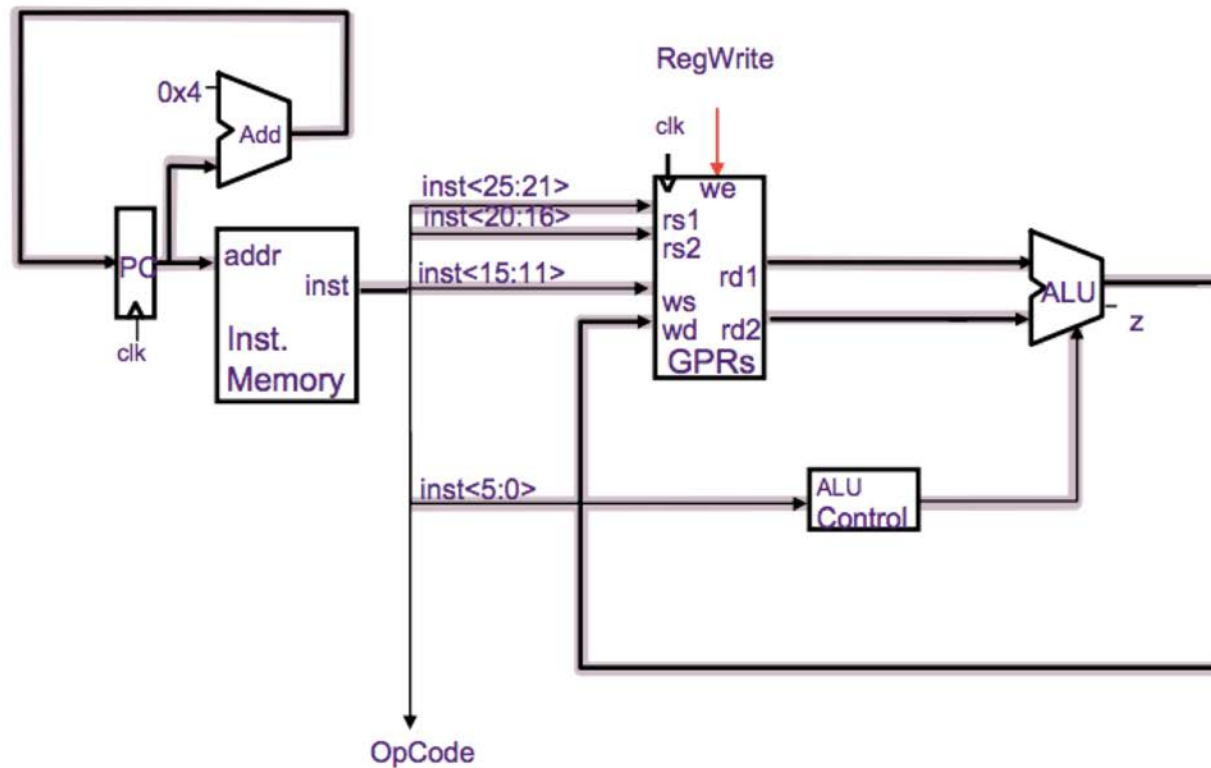
op	immediate26
----	-------------

		source(s)	destination
ALU	$rd \leftarrow (rs) \text{ func } (rt)$	rs, rt	rd
ALUi	$rt \leftarrow (rs) \text{ op } \text{imm}$	rs	rt
LW	$rt \leftarrow M [(rs) + \text{imm}]$	rs	rt
SW	$M [(rs) + \text{imm}] \leftarrow (rt)$	rs, rt	
BZ	cond (rs)		
	true: $PC \leftarrow (PC) + \text{imm}$	rs	
	false: $PC \leftarrow (PC) + 4$	rs	
J	$PC \leftarrow (PC) + \text{imm}$		
JAL	$r31 \leftarrow (PC), PC \leftarrow (PC) + \text{imm}$		31
JR	$PC \leftarrow (rs)$	rs	
JALR	$r31 \leftarrow (PC), PC \leftarrow (rs)$	rs	31

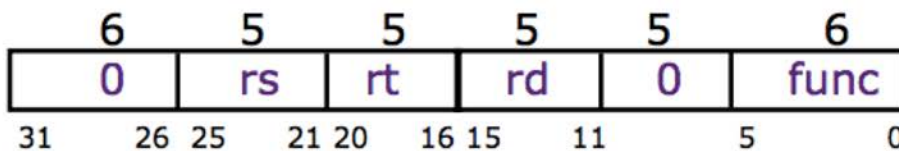
› Execution of an instruction involves

1. instruction fetch
2. decode and register fetch
3. ALU operation
4. memory operation (optional)
5. write back

and the computation of the address of the next instruction

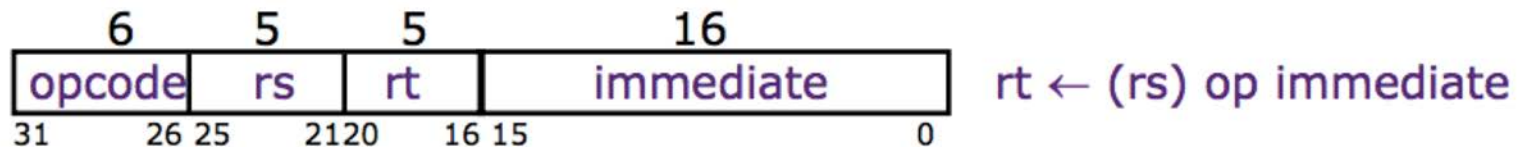
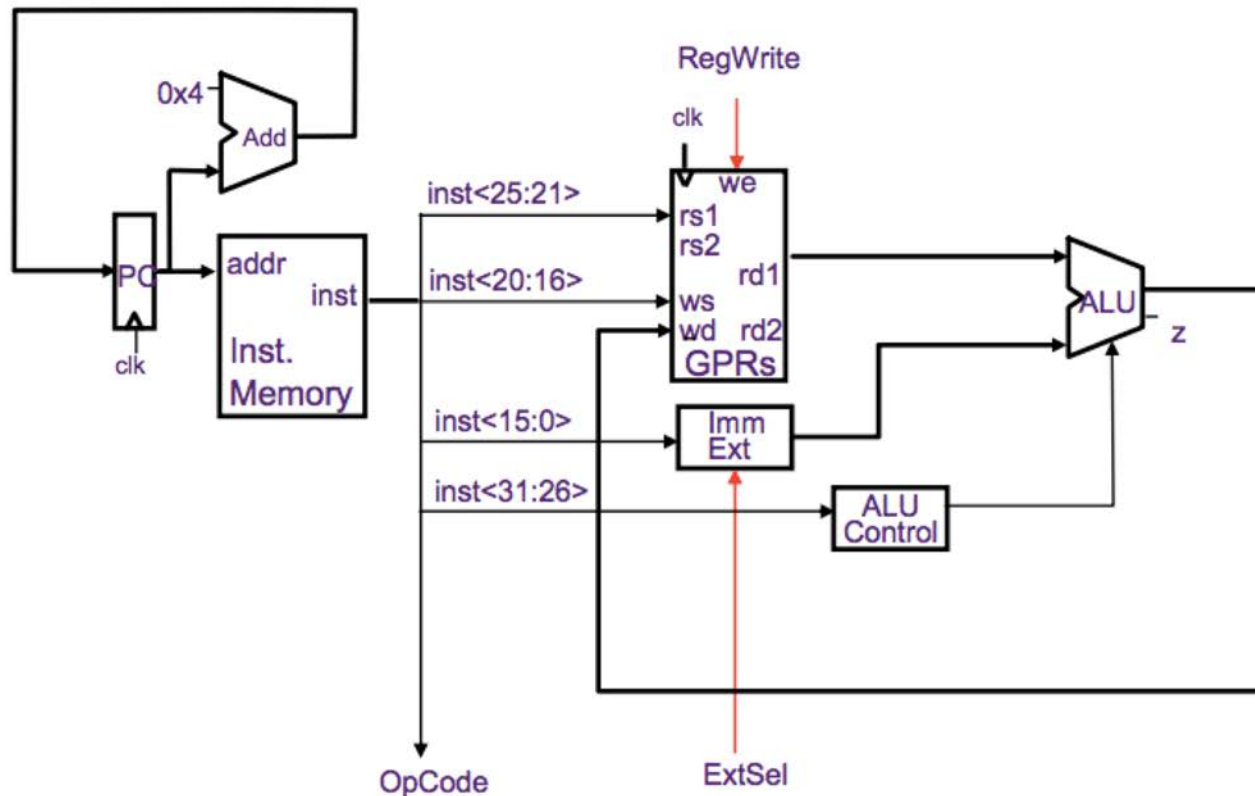


RegWrite Timing?

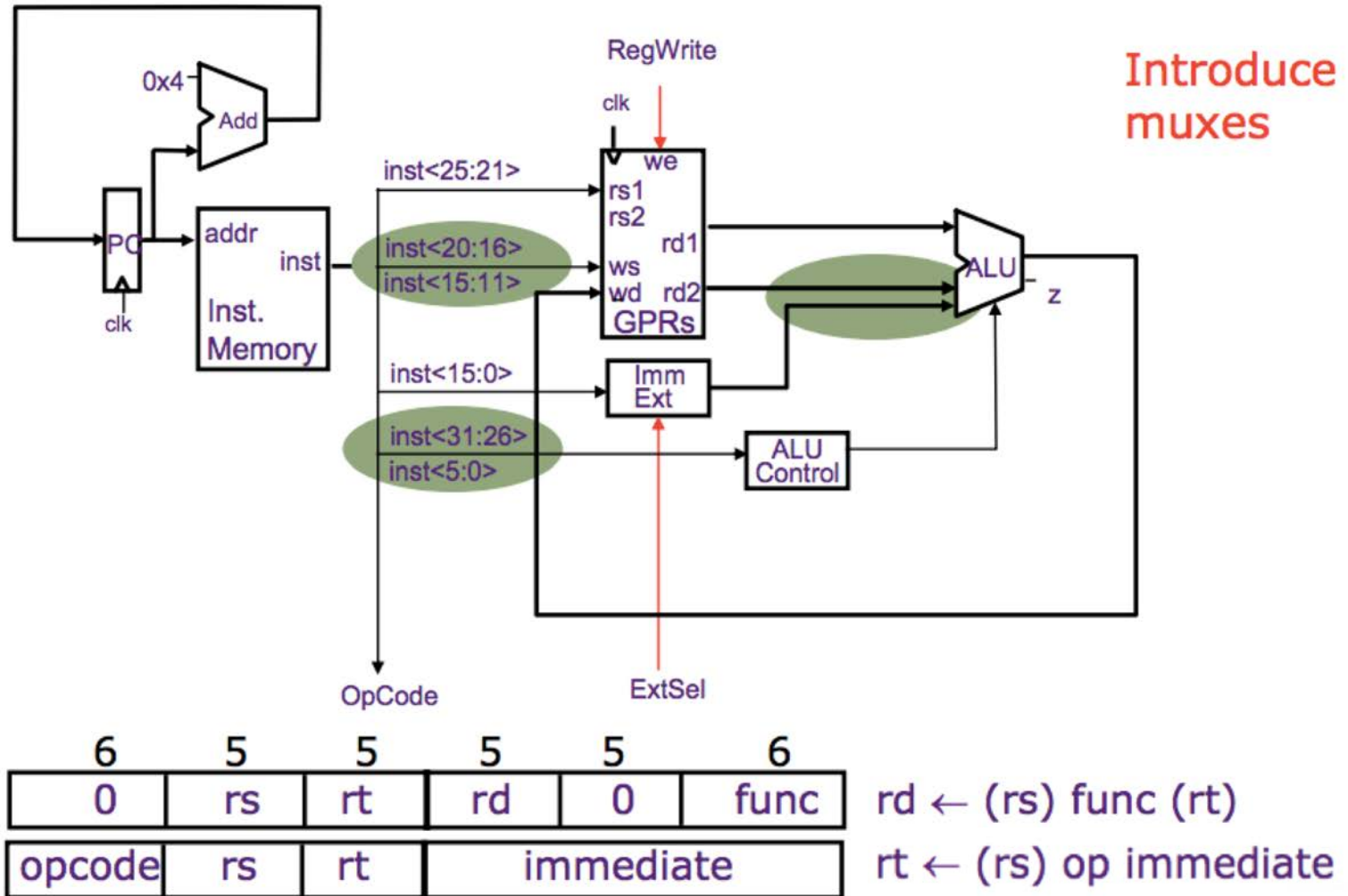


$$rd \leftarrow (rs) \text{ func } (rt)$$

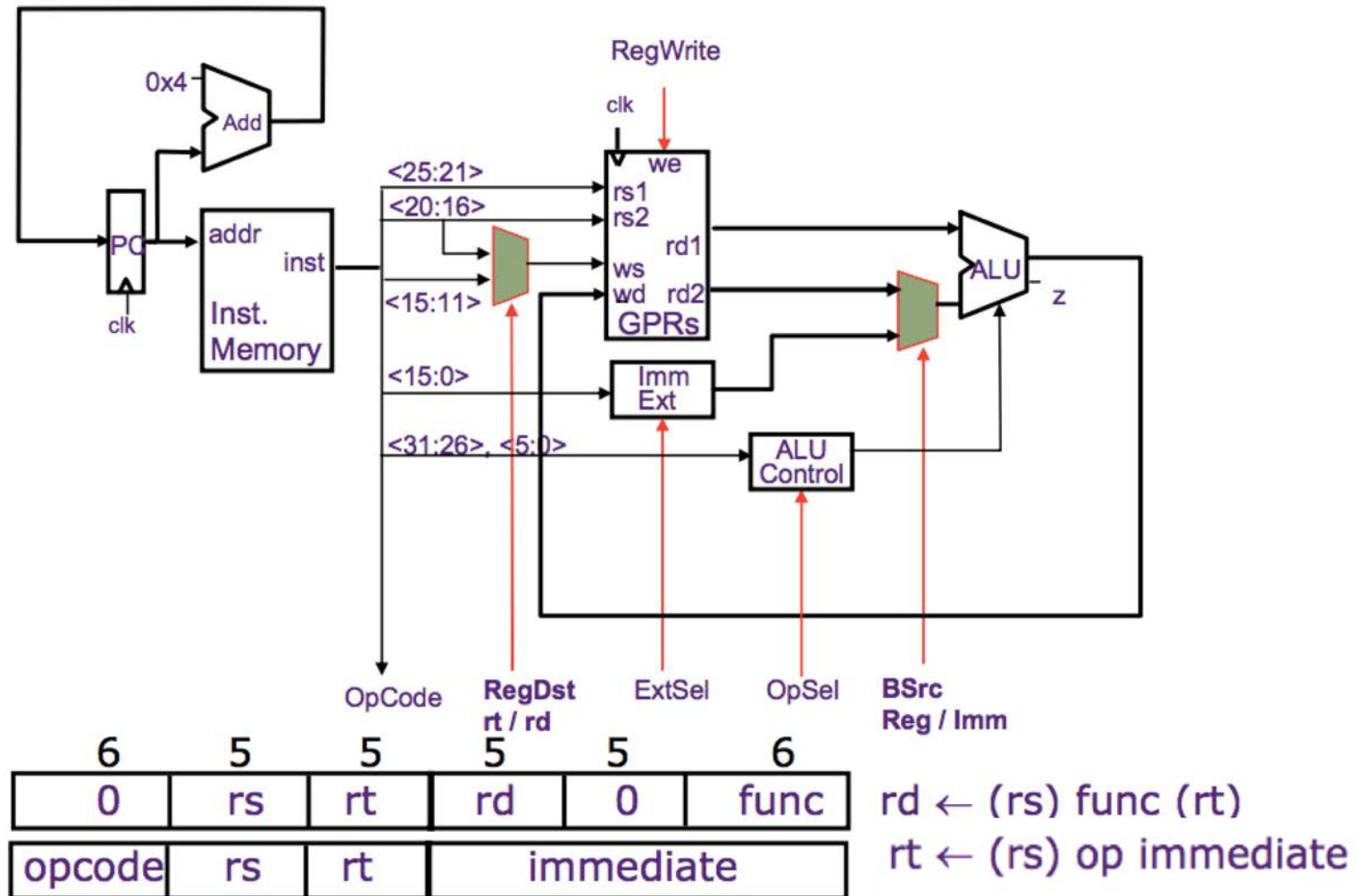
Datapath: Reg-Imm Instructions



Conflicts in Merging Datapath



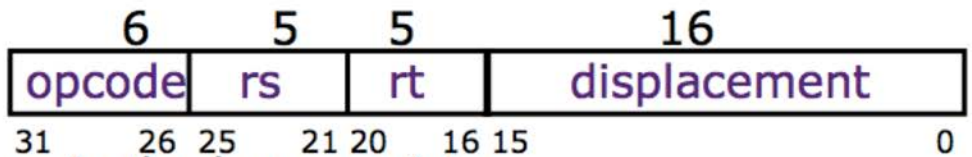
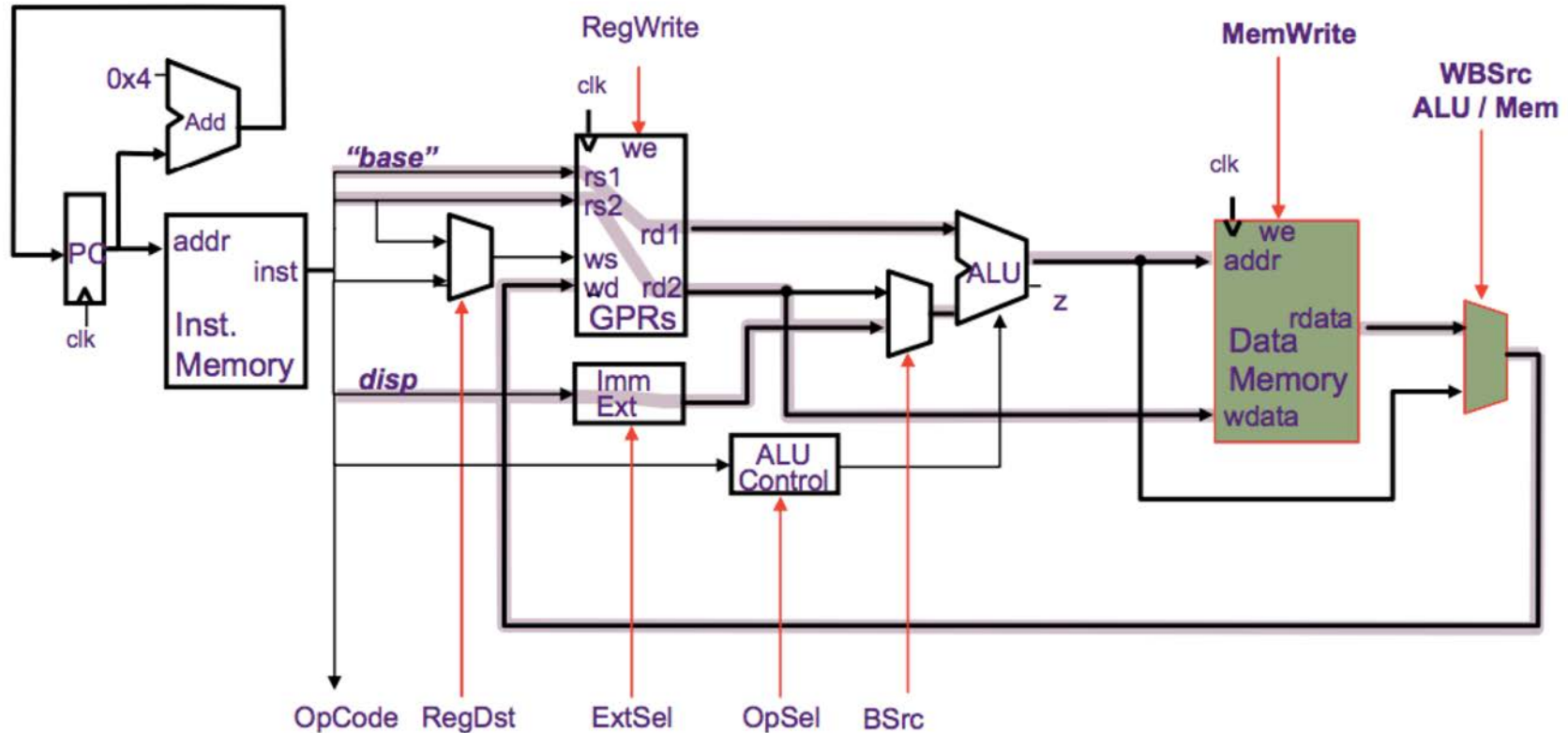
Datapath for ALU Instructions



- › Should program and data memory be separate?
- › Harvard style: separate (Aiken and Mark 1 influence)
 - read-only program memory
 - read/write data memory
 - at some level the two memories have to be the same
- › Princeton style: the same (von Neumann's influence)
 - A Load or Store instruction requires accessing the memory more than once during its execution



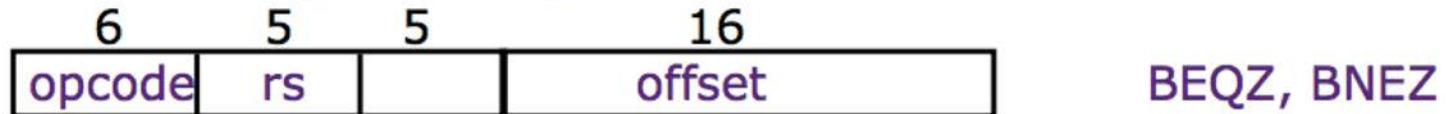
Load/Store Instructions: Harvard Architecture



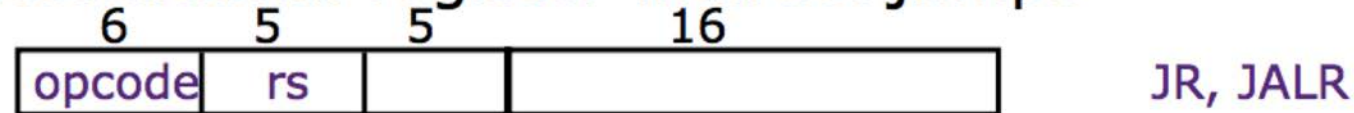
addressing mode
(rs) + displacement

rs is the base register
rt is the destination of a Load or the source for a Store

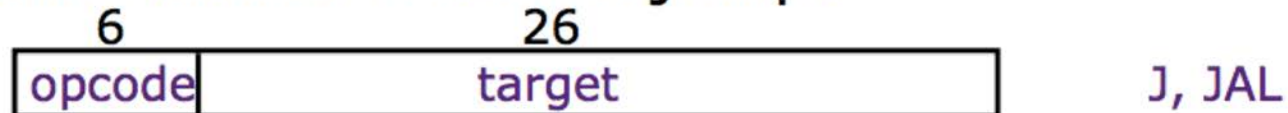
Conditional (on GPR) PC-relative branch



Unconditional register-indirect jumps

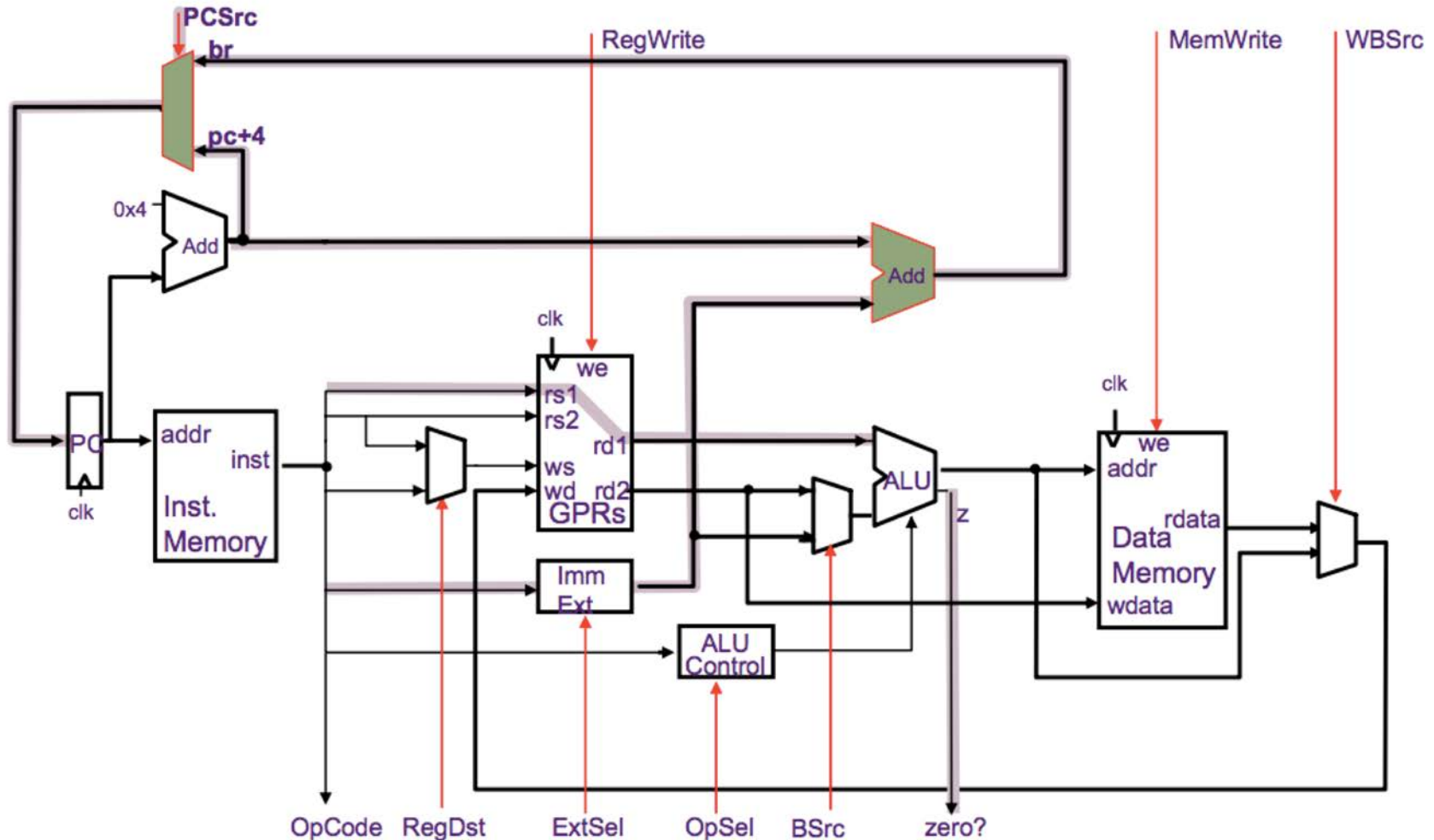


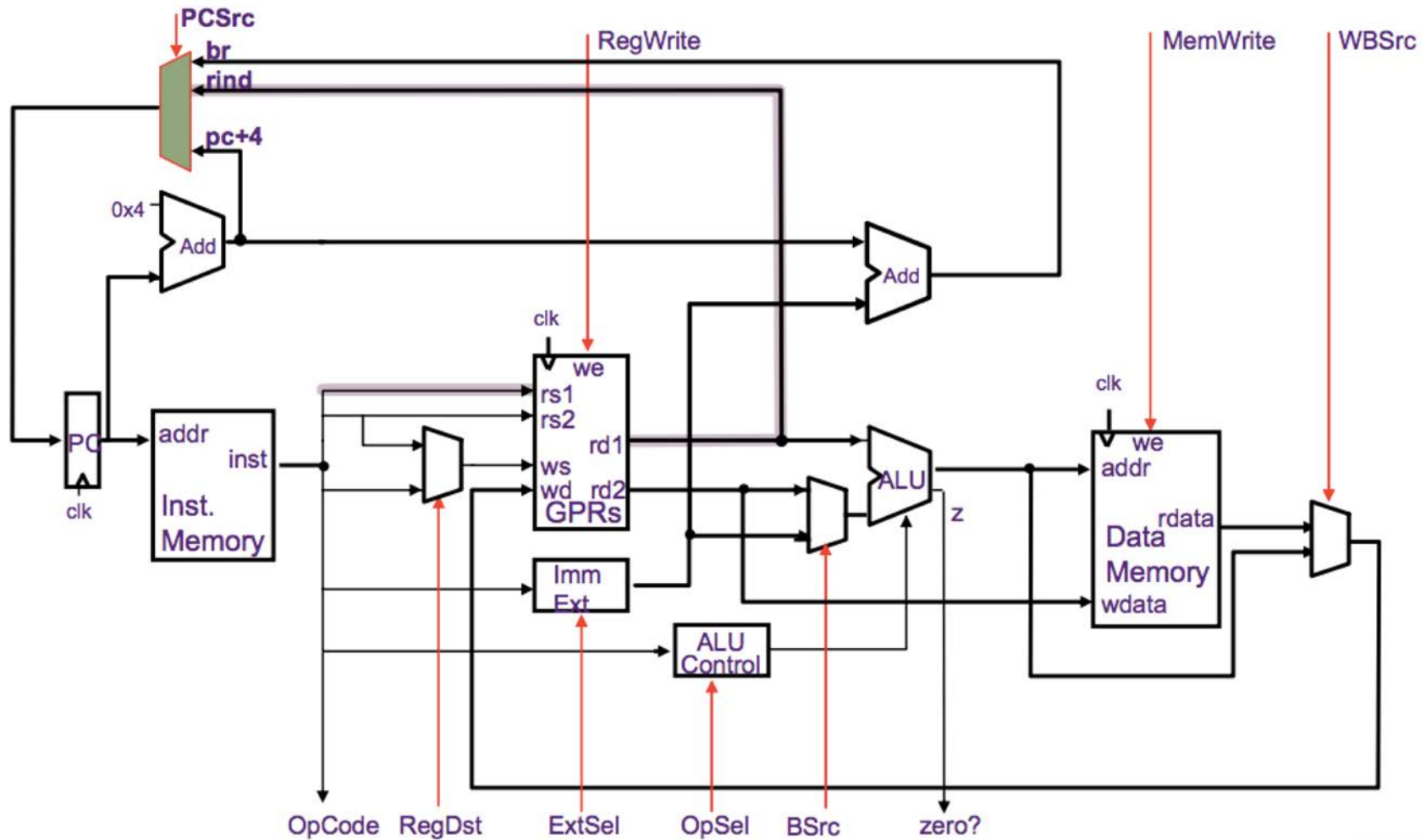
Unconditional absolute jumps



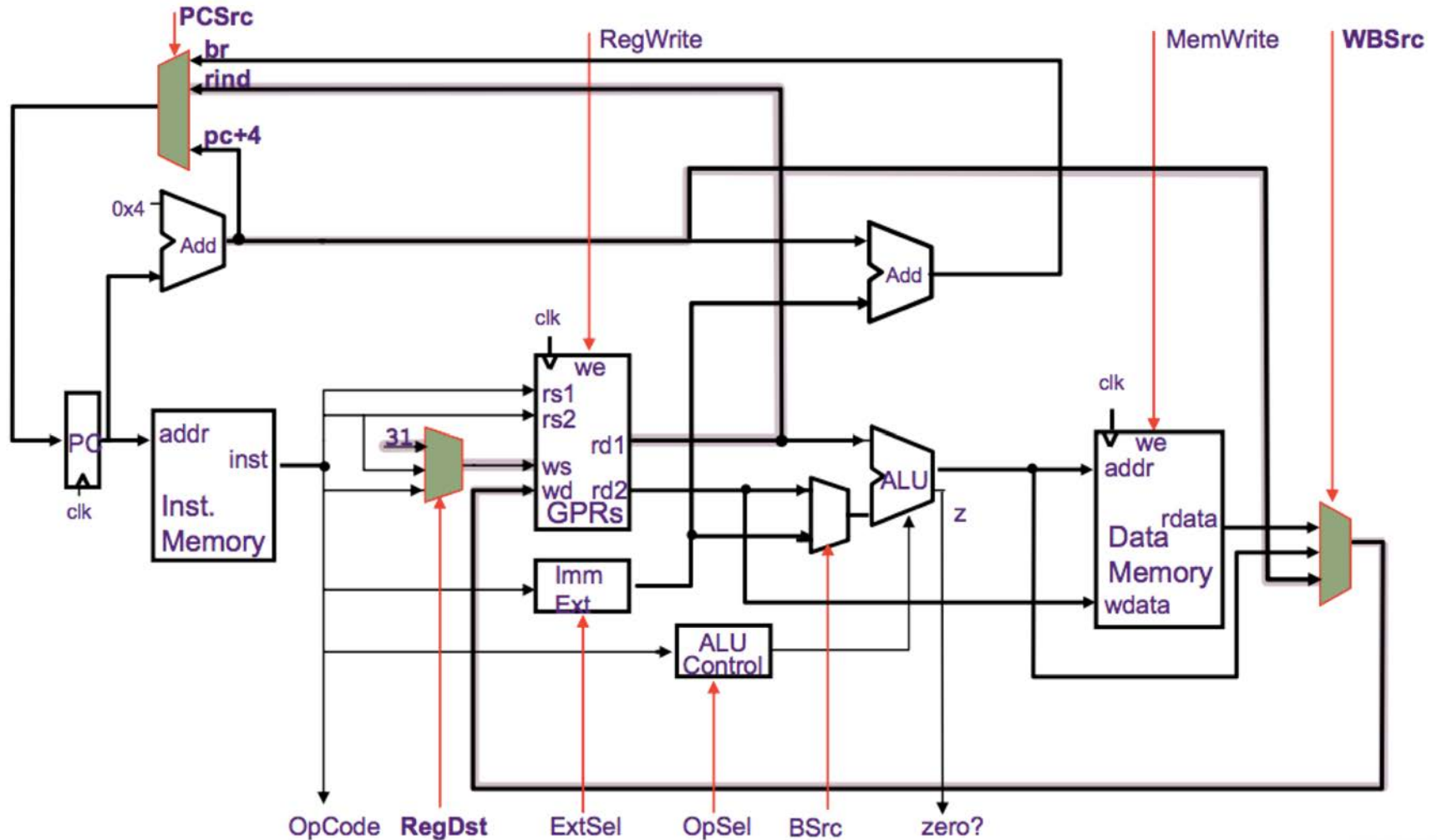
- PC-relative branches add $\text{offset} \times 4$ to $\text{PC}+4$ to calculate the target address (offset is in words): ± 128 KB range
- Absolute jumps append $\text{target} \times 4$ to $\text{PC}\langle 31:28 \rangle$ to calculate the target address: 256 MB range
- jump-&-link stores $\text{PC}+4$ into the link register (R31)
- All Control Transfers are delayed by 1 instruction
we will worry about the branch delay slot later

Conditional Branches (BEQZ, BNEZ)

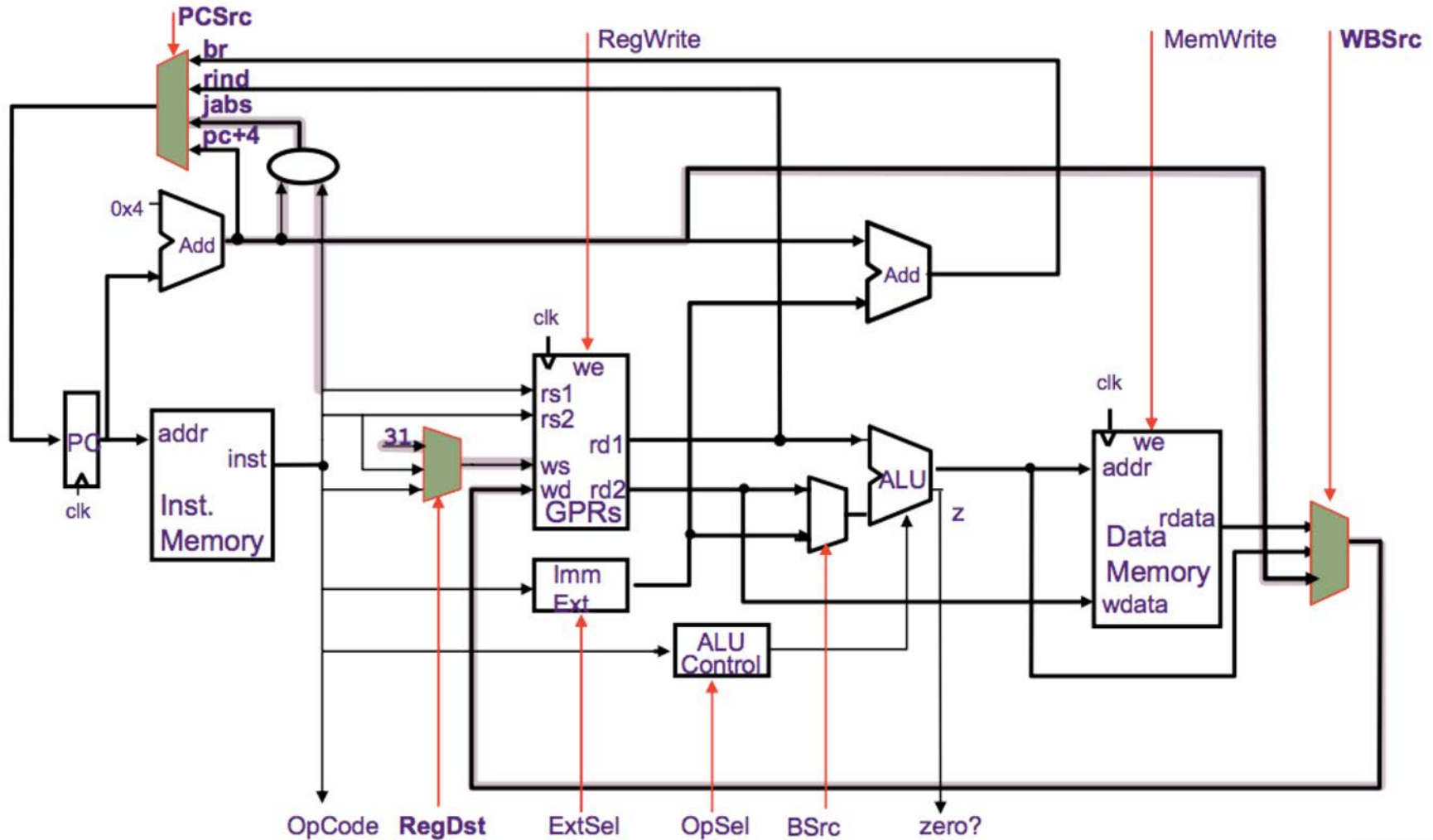




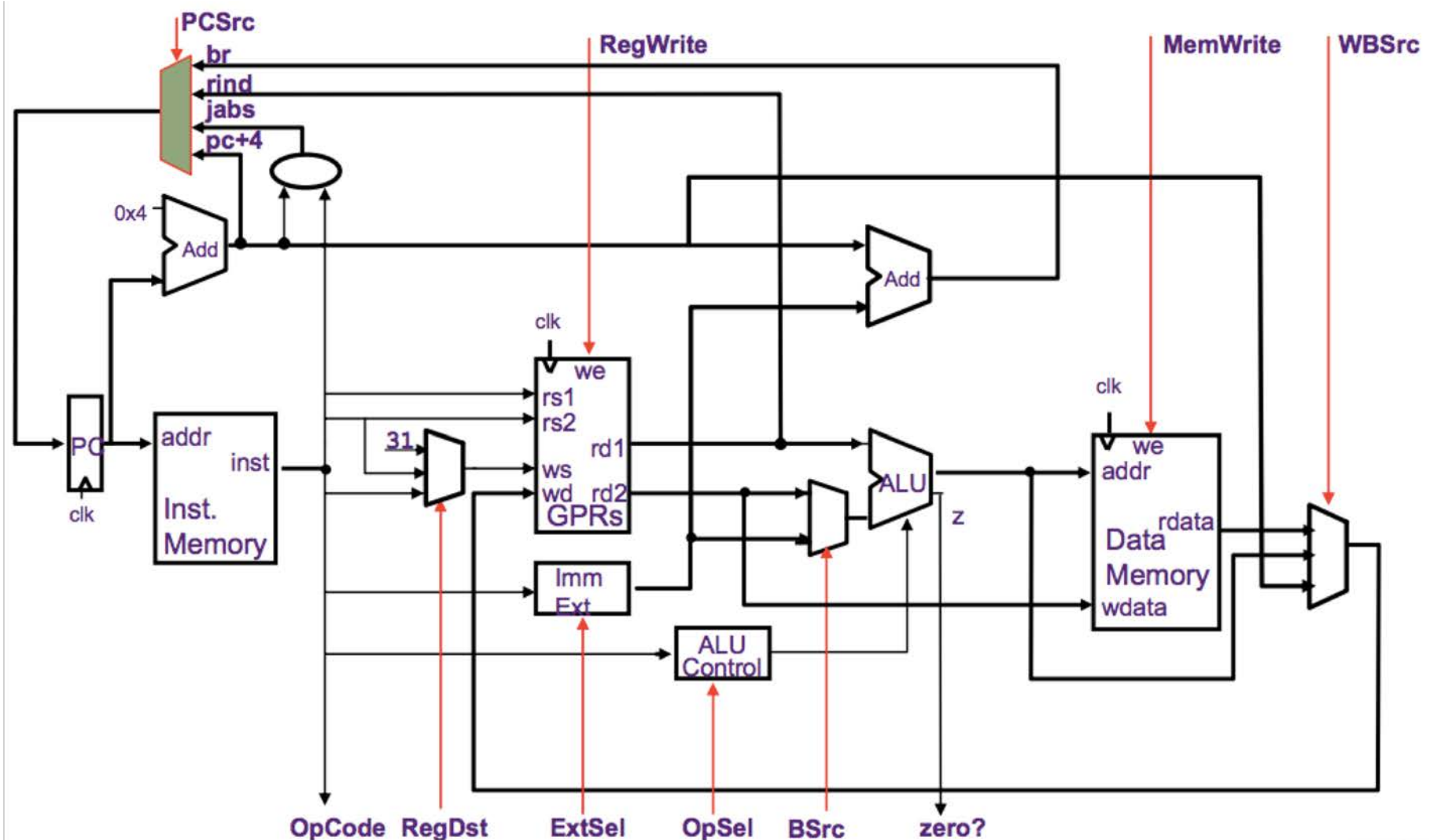
Register-Indirect Jump-&-Link (JALR)



Absolute Jumps (J, JAL)



Harvard-Style Datapath for MIPS



Control for Single Cycle RISC Processor

› We will assume

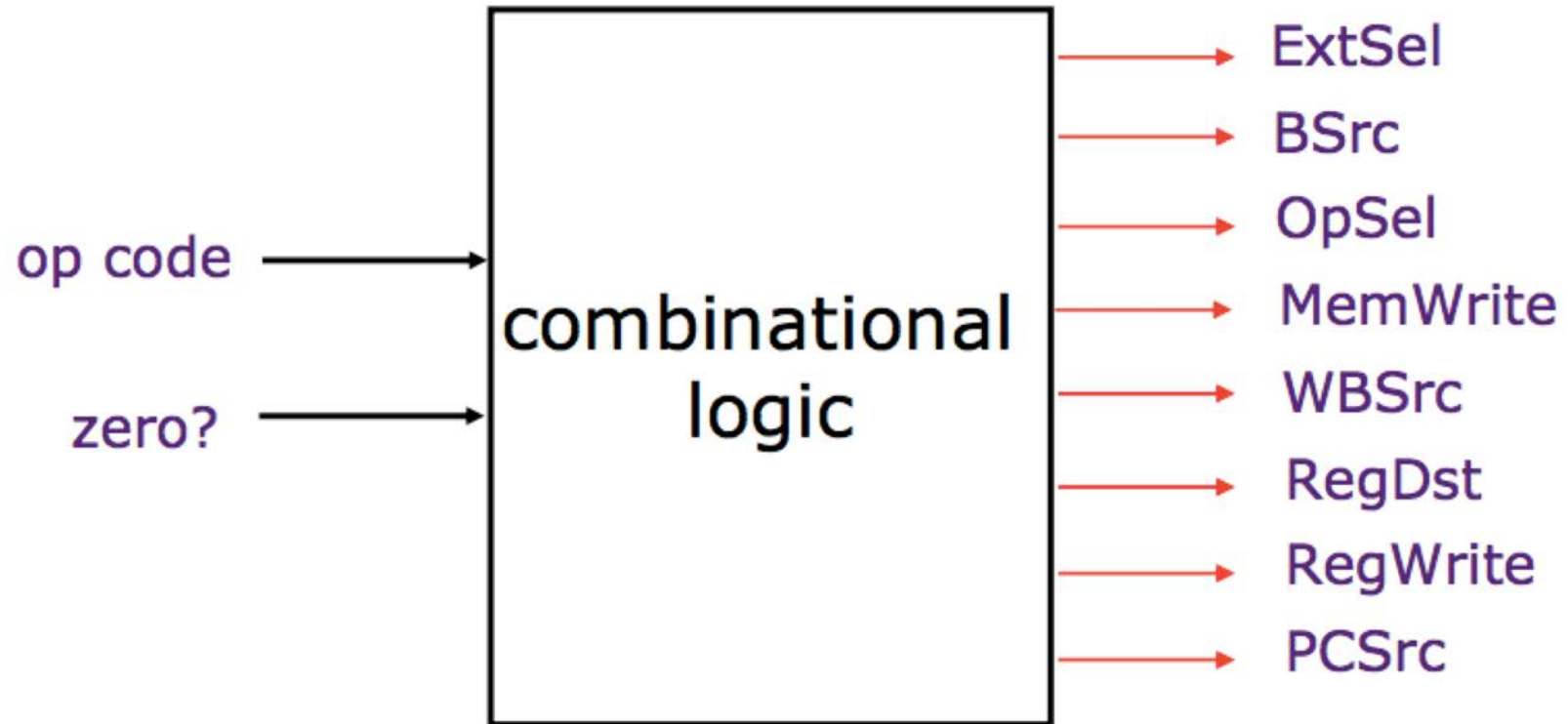
- clock period is sufficiently long for all of the following steps to be “completed”:

1. instruction fetch
2. decode and register fetch
3. ALU operation
4. data fetch if required
5. register write-back setup time

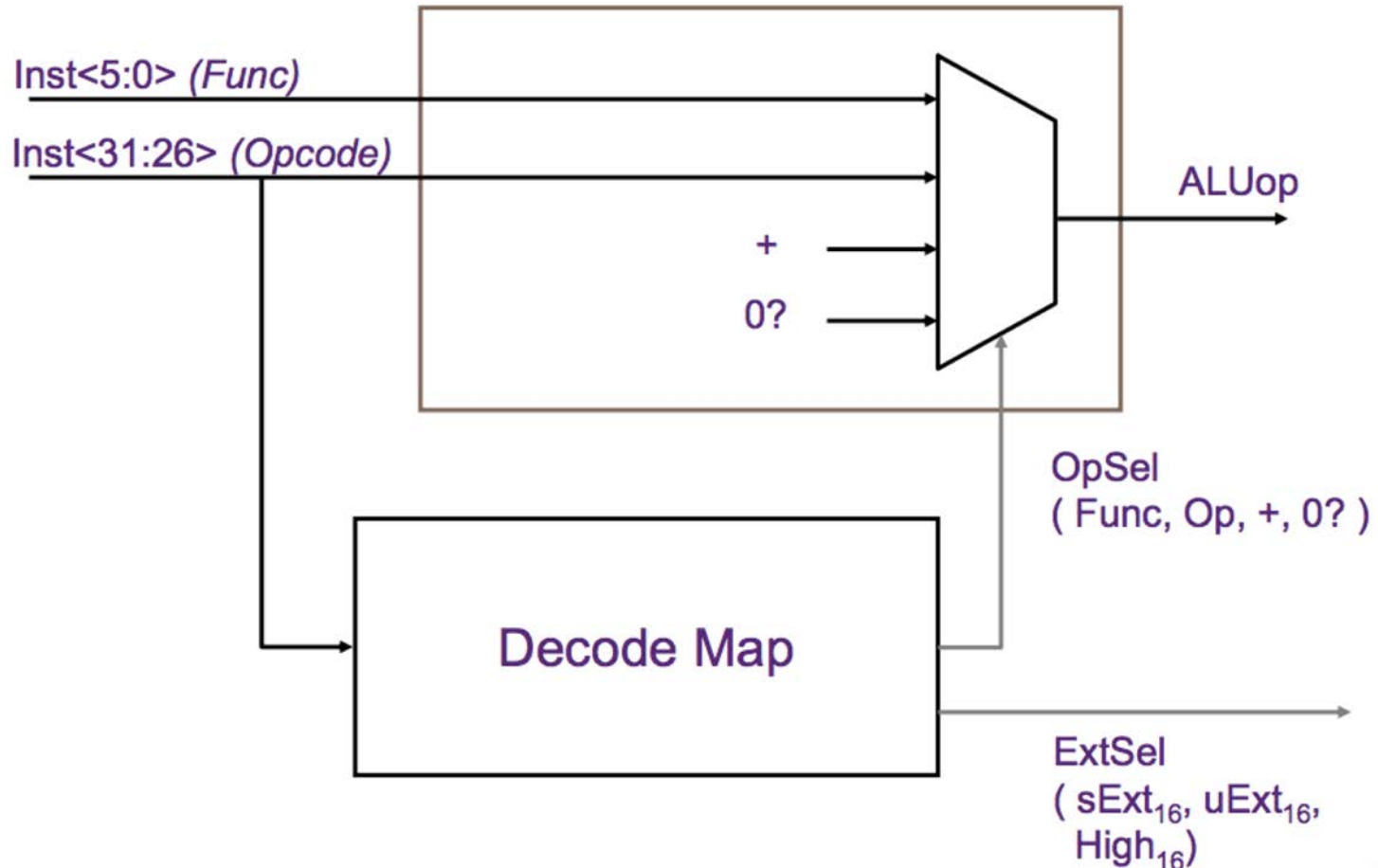
$$\Rightarrow \square t_C > t_{IFetch} + t_{RFetch} + t_{ALU} + t_{DMem} + t_{RWB}$$

- At the rising edge of the following clock, the PC, the register file and the memory are updated

Hardwired Control is pure Combinational Logic



ALU Control & Immediate Extension



Opcode	ExtSel	BSrc	OpSel	MemW	RegW	WBSrc	RegDst	PCSrc
ALU	*	Reg	Func	no	yes	ALU	rd	pc+4
ALUi	sExt ₁₆	Imm	Op	no	yes	ALU	rt	pc+4
ALUiu	uExt ₁₆	Imm	Op	no	yes	ALU	rt	pc+4
LW	sExt ₁₆	Imm	+	no	yes	Mem	rt	pc+4
SW	sExt ₁₆	Imm	+	yes	no	*	*	pc+4
BEQZ _{z=0}	sExt ₁₆	*	0?	no	no	*	*	br
BEQZ _{z=1}	sExt ₁₆	*	0?	no	no	*	*	pc+4
J	*	*	*	no	no	*	*	jabs
JAL	*	*	*	no	yes	PC	R31	jabs
JR	*	*	*	no	no	*	*	rind
JALR	*	*	*	no	yes	PC	R31	rind

BSrc = Reg / Imm

WBSrc = ALU / Mem / PC

RegDst = rt / rd / R31

PCSrc = pc+4 / br / rind / jabs

RISC Processor in Chisel



- › Go over the design of a simple RISC processor in Chisel
- › Code if from the chisel-tutorial Risc.scala example

```
package TutorialExamples
```

```
import Chisel._
```

```
class Risc extends Module {
```

```
  val io = new Bundle {
```

```
    val isWr  = Bool(INPUT)
```

```
    val wrAddr = UInt(INPUT, 8)
```

```
    val wrData = Bits(INPUT, 32)
```

```
    val boot  = Bool(INPUT)
```

```
    val valid = Bool(OUTPUT)
```

```
    val out   = Bits(OUTPUT, 32)
```

```
  }
```

```
  val file = Mem(Bits(width = 32), 256)
```

```
  val code = Mem(Bits(width = 32), 256)
```

```
  val pc   = Reg(init=UInt(0, 8))
```

```
  val add_op :: imm_op :: Nil = Enum(Bits(), 2)
```

```
  val inst = code(pc)
```

```
  val op   = inst(31,24)
```

```
  val rci  = inst(23,16)
```

```
  val rai  = inst(15, 8)
```

```
  val rbi  = inst( 7, 0)
```

```
  val ra = Mux(rai === Bits(0), Bits(0), file(rai))
```

```
  val rb = Mux(rbi === Bits(0), Bits(0), file(rbi))
```

```
  val rc = Bits(width = 32)
```

```
io.valid := Bool(false)
```

```
io.out := Bits(0)
```

```
rc := Bits(0)
```

```
when (io.isWr) {
```

```
  code(io.wrAddr) := io.wrData
```

```
} .elsewhen (io.boot) {
```

```
  pc := UInt(0)
```

```
} .otherwise {
```

```
switch(op) {
```

```
  is(add_op) { rc := ra + rb }
```

```
  is(imm_op) { rc := (rai << UInt(8)) | rbi }
```

```
}
```

```
io.out := rc
```

```
when (rci === UInt(255)) {
```

```
  io.valid := Bool(true)
```

```
} .otherwise {
```

```
  file(rci) := rc
```

```
}
```

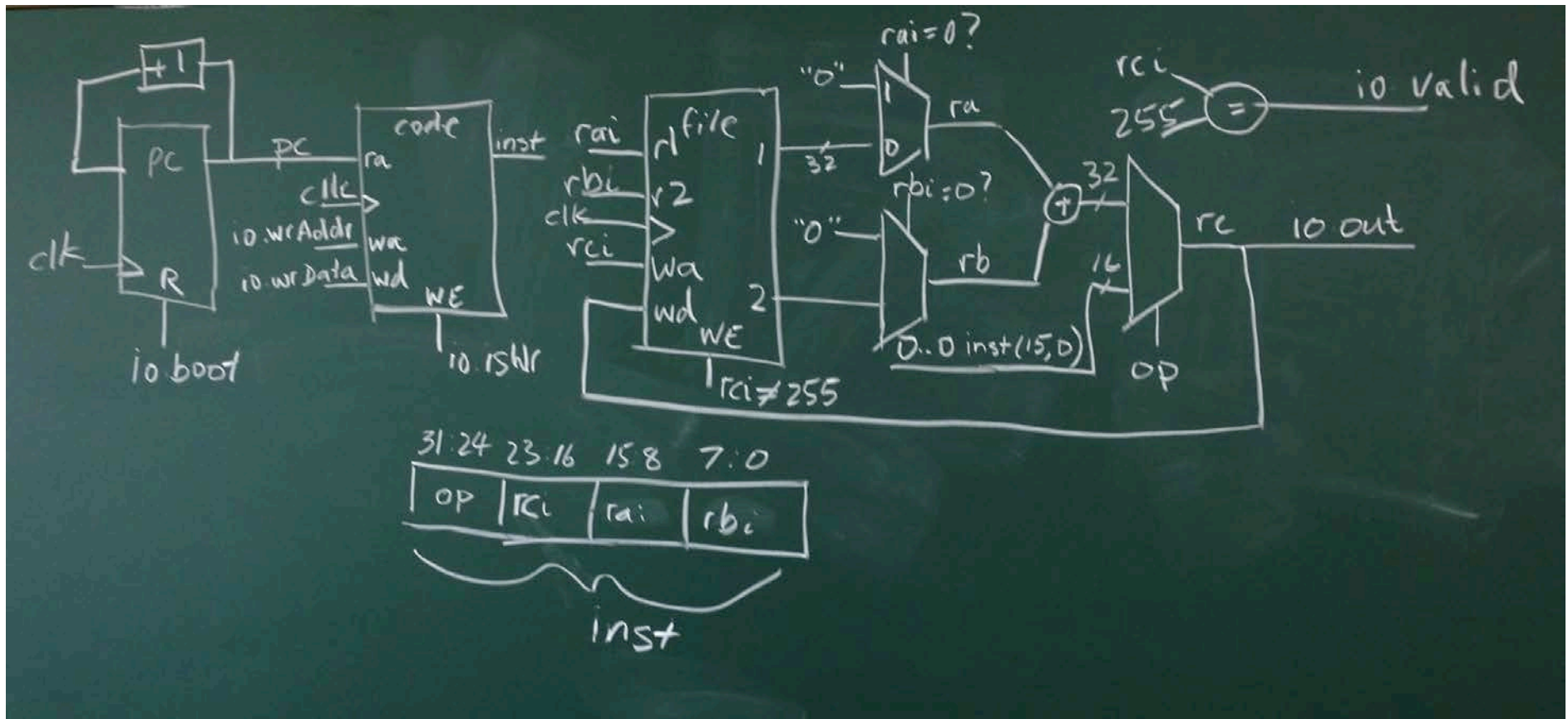
```
pc := pc + UInt(1)
```

```
}
```

```
}
```

```
class RiscTests(c: Risc) extends Tester(c) {  
  def wr(addr: UInt, data: UInt) = {  
    poke(c.io.isWr, 1)  
    poke(c.io.wrAddr, addr.litValue())  
    poke(c.io.wrData, data.litValue())  
    step(1)  
  }  
  def boot() = {  
    poke(c.io.isWr, 0)  
    poke(c.io.boot, 1)  
    step(1)  
  }  
  def tick() = {  
    poke(c.io.isWr, 0)  
    poke(c.io.boot, 0)  
    step(1)  
  }  
}
```

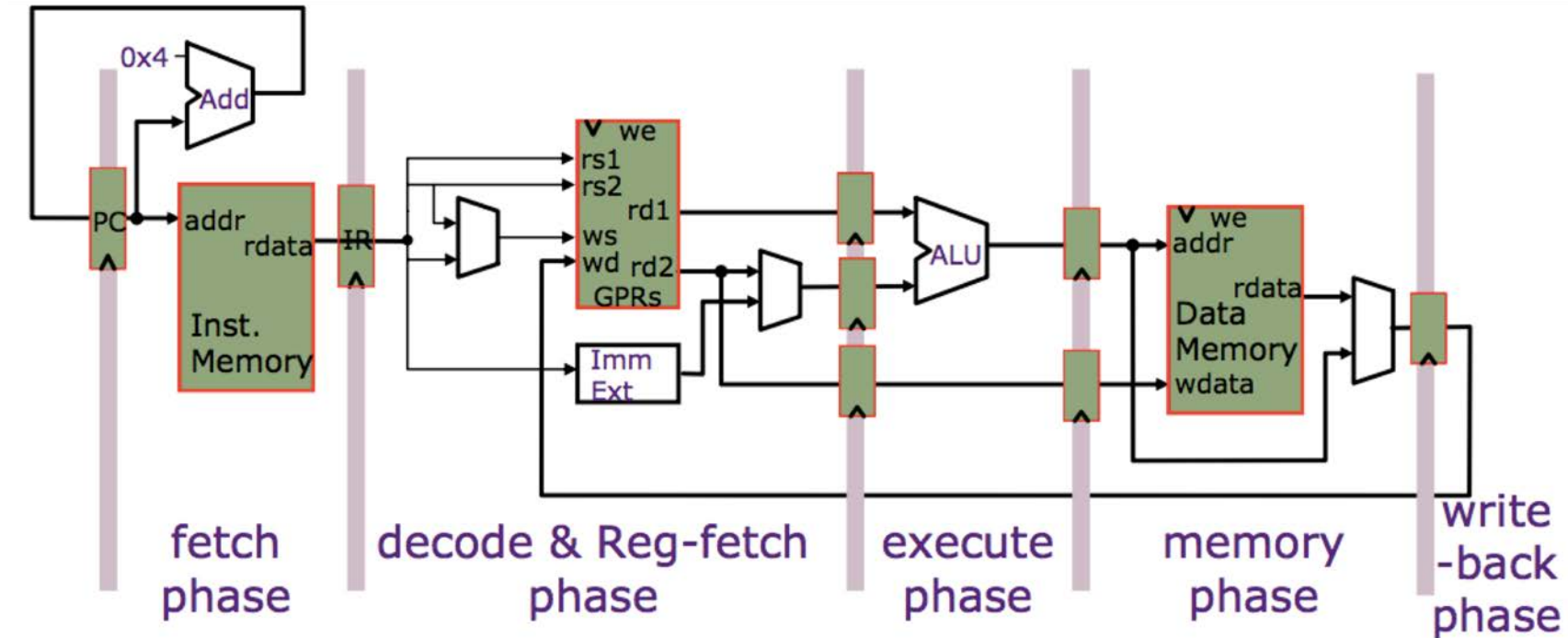
```
def l (op: UInt, rc: Int, ra: Int, rb: Int) =  
  Cat(op, UInt(rc, 8), UInt(ra, 8), UInt(rb, 8))  
val app = Array(l(c.imm_op, 1, 0, 1), // r1 <- 1  
                l(c.add_op, 1, 1, 1), // r1 <- r1 + r1  
                l(c.add_op, 1, 1, 1), // r1 <- r1 + r1  
                l(c.add_op, 255, 1, 0)) // rh <- r1  
wr(UInt(0), Bits(0)) // skip reset  
for (addr <- 0 until app.length)  
  wr(UInt(addr), app(addr))  
boot()  
var k = 0  
do {  
  tick(); k += 1  
} while (peek(c.io.valid) == 0 && k < 10)  
expect(k < 10, "TIME LIMIT")  
expect(c.io.out, 4)  
}
```



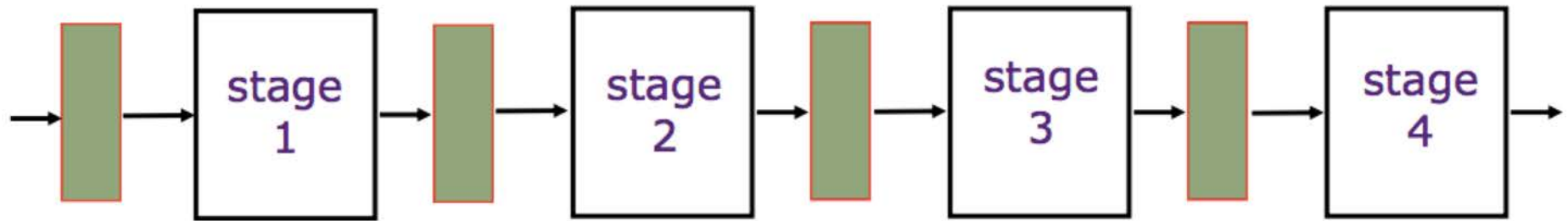
Pipelined RISC Processor



- › To pipeline MIPS:
 - First build MIPS without pipelining with $CPI=1$
 - Next, add pipeline registers to reduce cycle time while maintaining $CPI=1$



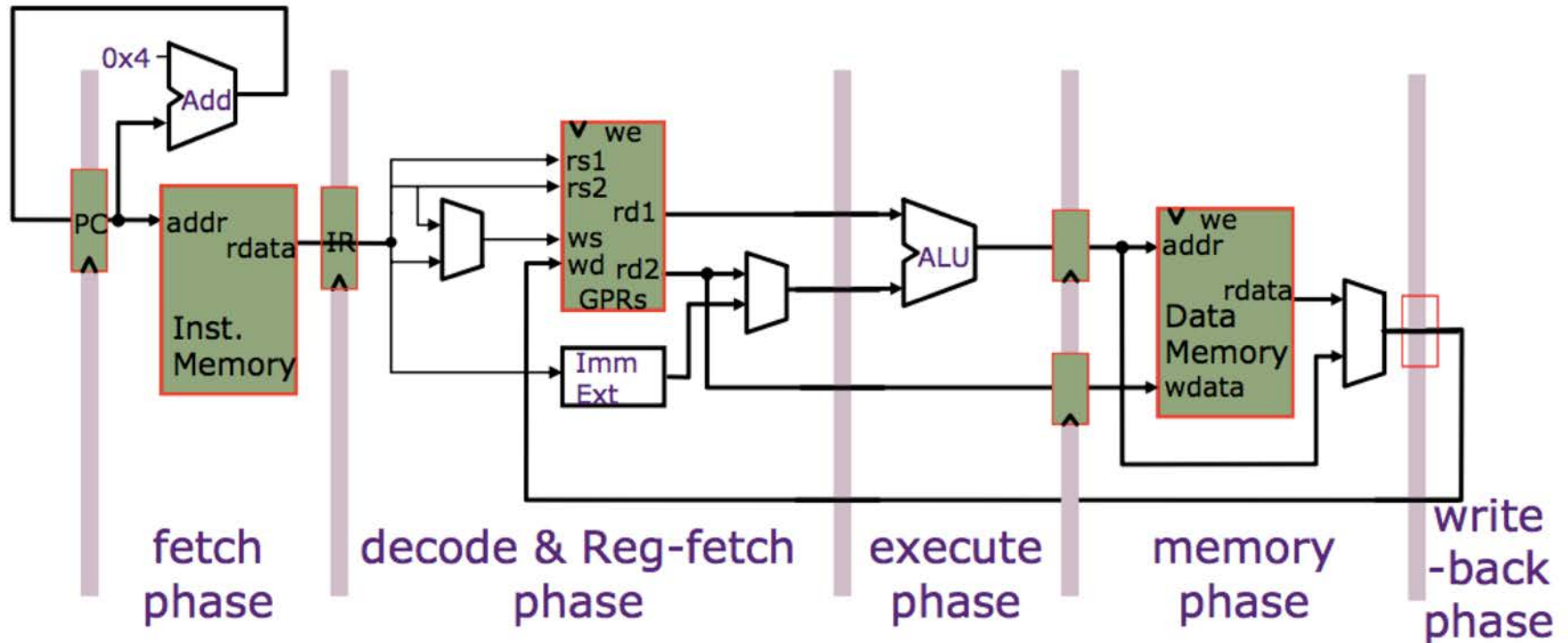
- › Clock period can be reduced by dividing the execution of an instruction into multiple cycles
- › $t_C > \max \{t_{IM}, t_{RF}, t_{ALU}, t_{DM}, t_{RW}\}$ (= t_{DM} probably)
- › However, CPI will increase unless instructions are pipelined



- › All objects go through the same stages
 - No sharing of resources between any two stages
 - Propagation delay through all pipeline stages is equal
 - The scheduling of an object entering the pipeline is not affected by the objects in other stages
- › These conditions generally hold for industrial assembly lines.
- › But can an instruction pipeline satisfy the last condition?

How to divide the datapath into stages

- › Suppose memory is significantly slower than other stages. In particular, suppose
 - $t = 10$ units IM
 - $t = 10$ units DM
 - $t = 5$ units ALU
 - $t = 1$ unit RF
 - $t = 1$ unit RW
- › Since the slowest stage determines the clock, it may be possible to combine some stages without any loss of performance



$$t_C > \max \{t_{IM}, t_{RF}+t_{ALU}, t_{DM}+t_{RW}\} = t_{DM} + t_{RW}$$

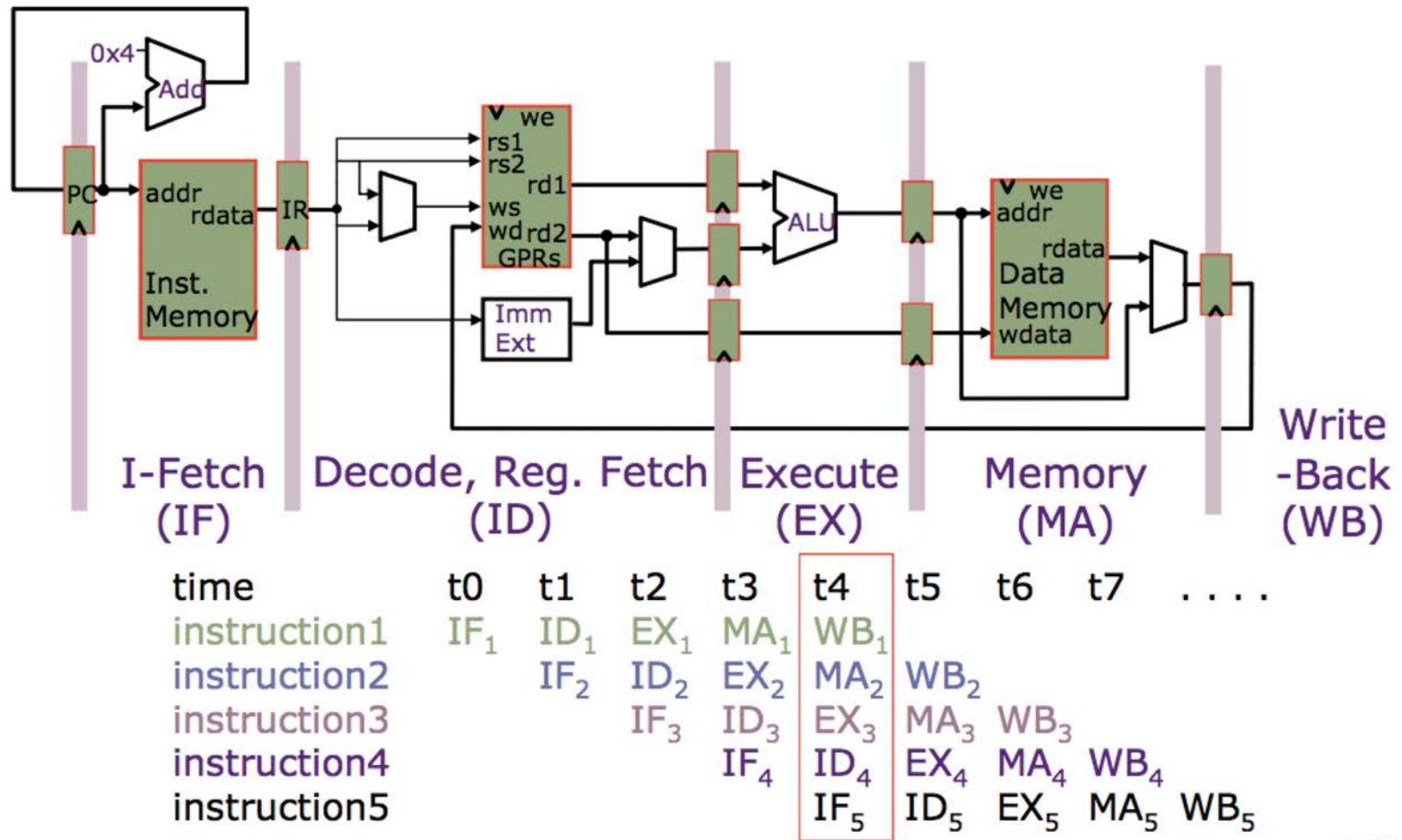
⇒ increase the critical path by 10%

Write-back stage takes much less time than other stages.
Suppose we combined it with the memory phase

Maximum Speedup from Pipelining

Assumptions	Unpipelined t_c	Pipelined t_c	Speedup
1. $t_{IM} = t_{DM} = 10,$ $t_{ALU} = 5,$ $t_{RF} = t_{RW} = 1$ 4-stage pipeline	27	10	2.7
2. $t_{IM} = t_{DM} = t_{ALU} = t_{RF} = t_{RW} = 5$ 4-stage pipeline	25	10	2.5
3. $t_{IM} = t_{DM} = t_{ALU} = t_{RF} = t_{RW} = 5$ 5-stage pipeline	25	5	5.0

It is possible to achieve higher speedup with more stages in the pipeline.



- › Design of a simple RISC processor
 - First you design datapath and then add control
 - All designs (serial, parallel) or otherwise follow a similar methodology
- › Not covered
 - What happens if there are pipeline dependencies e.g. add r1, r2, r3; add r2, r1, r1
 - What happens if we branch e.g. add r1, r2, r3; beqz r1 loop
 - These are called hazards and can be resolved by stalling (low performance) and to some degree by forwarding (add internal paths to make data available earlier)
 - Refer to [1] and [2] for details

- › Draw the datapath and control for the Chisel RISC processor
- › Modify the Chisel RISC processor to have a 2 stage pipeline (instruction fetch and execution)

- [1] Patterson, D. A., and J. L. Hennessy. Computer Organization and Design: The Hardware/Software Interface, Morgan Kaufman.
- [2] Hennessy, J. L., and D. A. Patterson. Computer Architecture: A Quantitative Approach, Morgan Kaufman.